

# Frequency dependence of effective bottom attenuation due to environmental variability

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# Introduction

- Traditionally, ocean sediment attenuation assumes linear frequency dependence such that loss per distance has the form  $\mathbf{a} = bf$  (or constant loss per wavelength), where  $\alpha$  may have units 1/m or dB/m, and  $b$ =constant. Parameterization of sediment attenuation then relies on determination of  $b$ .
- More recent inversion studies (e.g., Zhou et al., 1987) have suggested non-linear frequency dependence of attenuation, i.e.,  $b = cf^x$  such that  $\mathbf{a} = cf^{(1+x)}$ . Zhou et al. found  $x \sim 0.7$ , so  $\mathbf{a} \propto f^{1.7}$
- Physical models of sediment attenuation mechanism unclear on inherent nonlinear response versus effective nonlinear response due to variable environmental influences.

# Model

- Monterey-Miami Parabolic Equation (MMPE) model used to compute propagation. Inputs may include range-dependent sound speed profiles, water-sediment and sediment-basement interfaces, sediment/basement sound speed gradients, sediment/basement sound speed and density fluctuations, and constant sediment/basement attenuation values (linear frequency dependence assumed).
- Sound speed profiles input deterministically.
- Interface roughness based on realizations of spectral model,

$$W_h(K) \propto (1 + L_h^2 K^2)^{-b}$$

- Sound speed/density variability based on realizations of spectral model

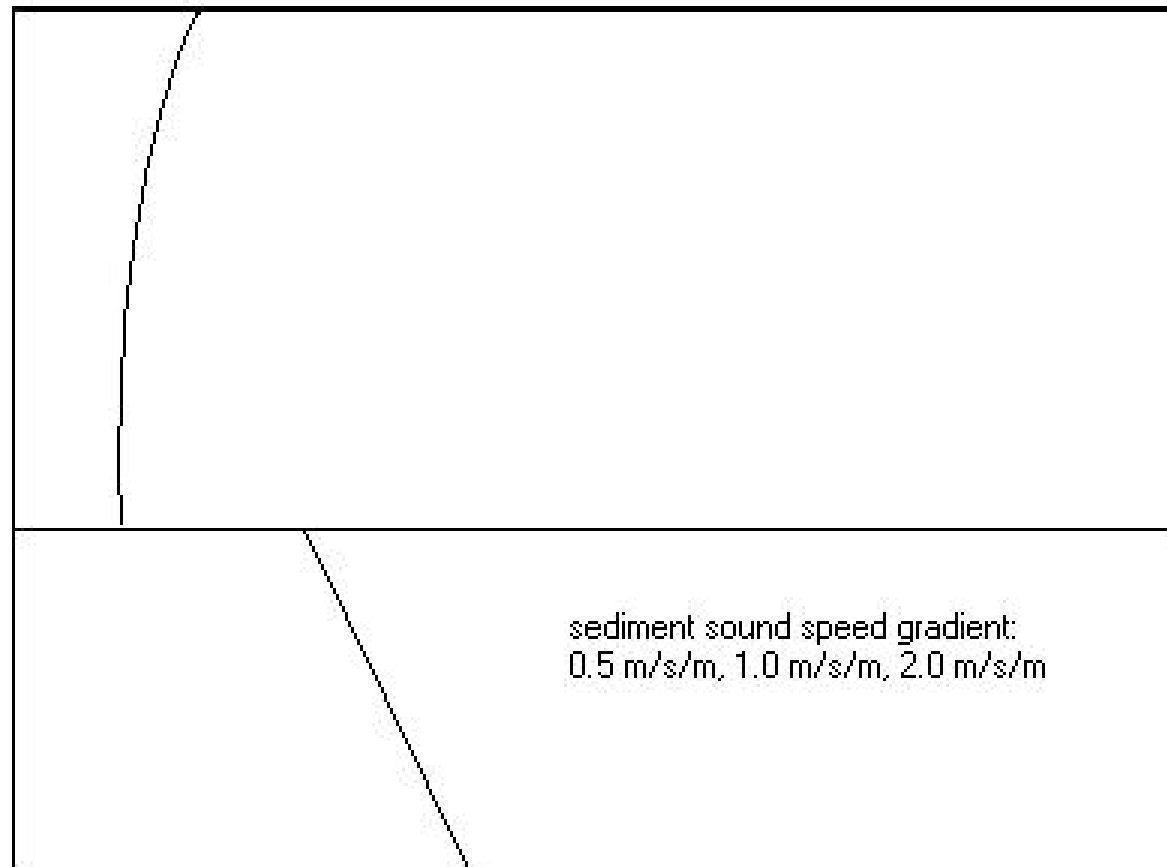
$$W_{dc}(K, M) \propto (\Lambda^2 K^2 + M^2)^{-g}$$

# Approach – Part I

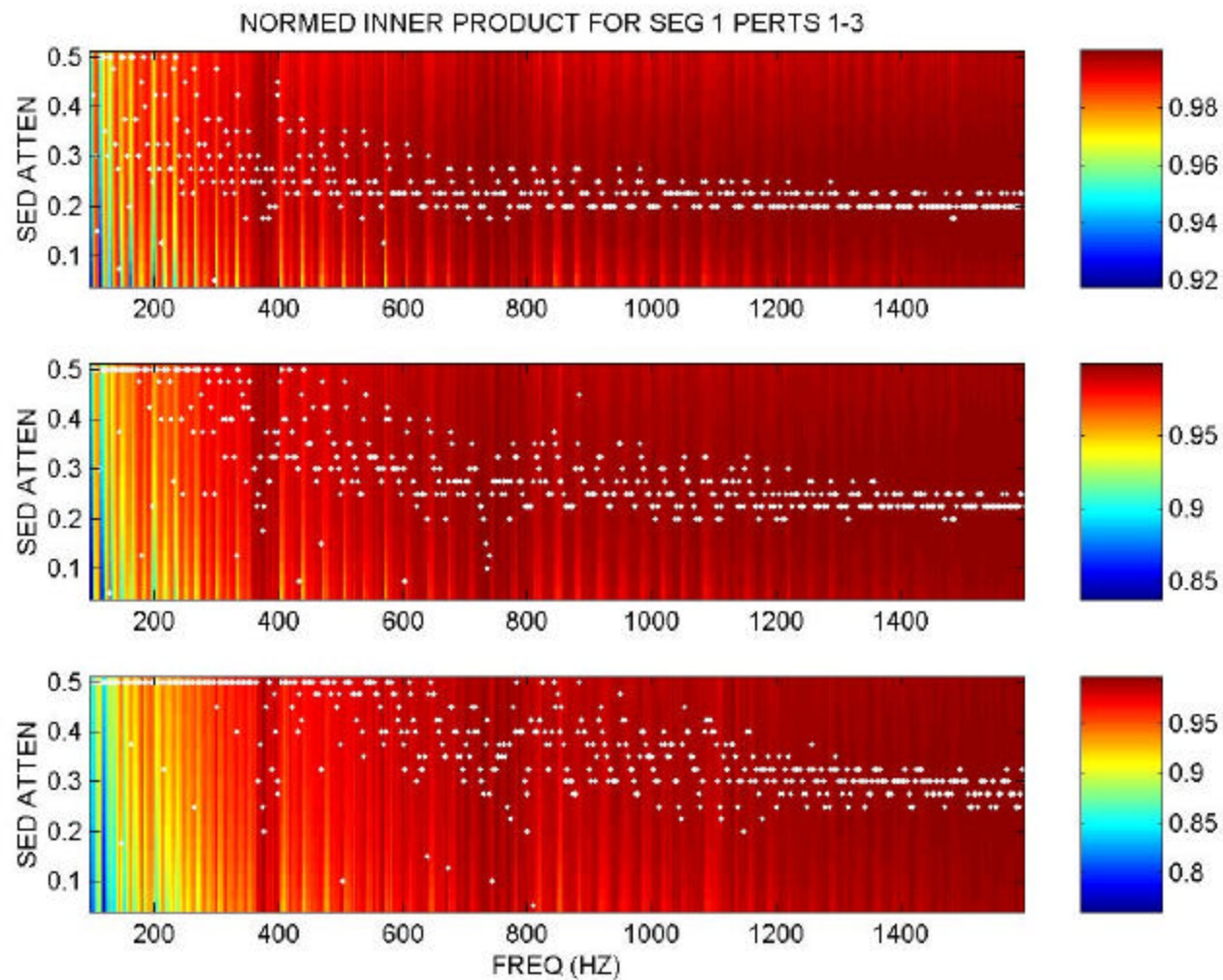
- Direct numerical evaluation of environmental fluctuations influence on effective frequency dependence as measured by simple, linear correlation analysis.
- MMPE model run assuming  $b_{\text{sed}} = 0.15$  dB/km/Hz for numerous environments containing perturbations. Results in complex pressure values at multiple depths:  $p(r, z_j)$  with  $r = 10$  km, and  $z_j$  containing 16 depths from 0 to 100 m.
- MMPE model then run for range-independent environment (avg SSP, no sediment gradient, all other values constant). Sediment attenuation then varies from  $b_{\text{sed}} = 0.025$  to 0.5 dB/km/Hz. Results in complex pressure replica matrix  $p_b'(r, z_j)$ .
- Effective attenuation determined by maximizing normalized correlation between pressure magnitudes over band of frequencies,

$$C(r, f, b) = \frac{\sum_j |p(r, z_j)| |p_b'(r, z_j)|}{\sqrt{\sum_j |p(r, z_j)|^2 \sum_j |p_b'(r, z_j)|^2}}$$

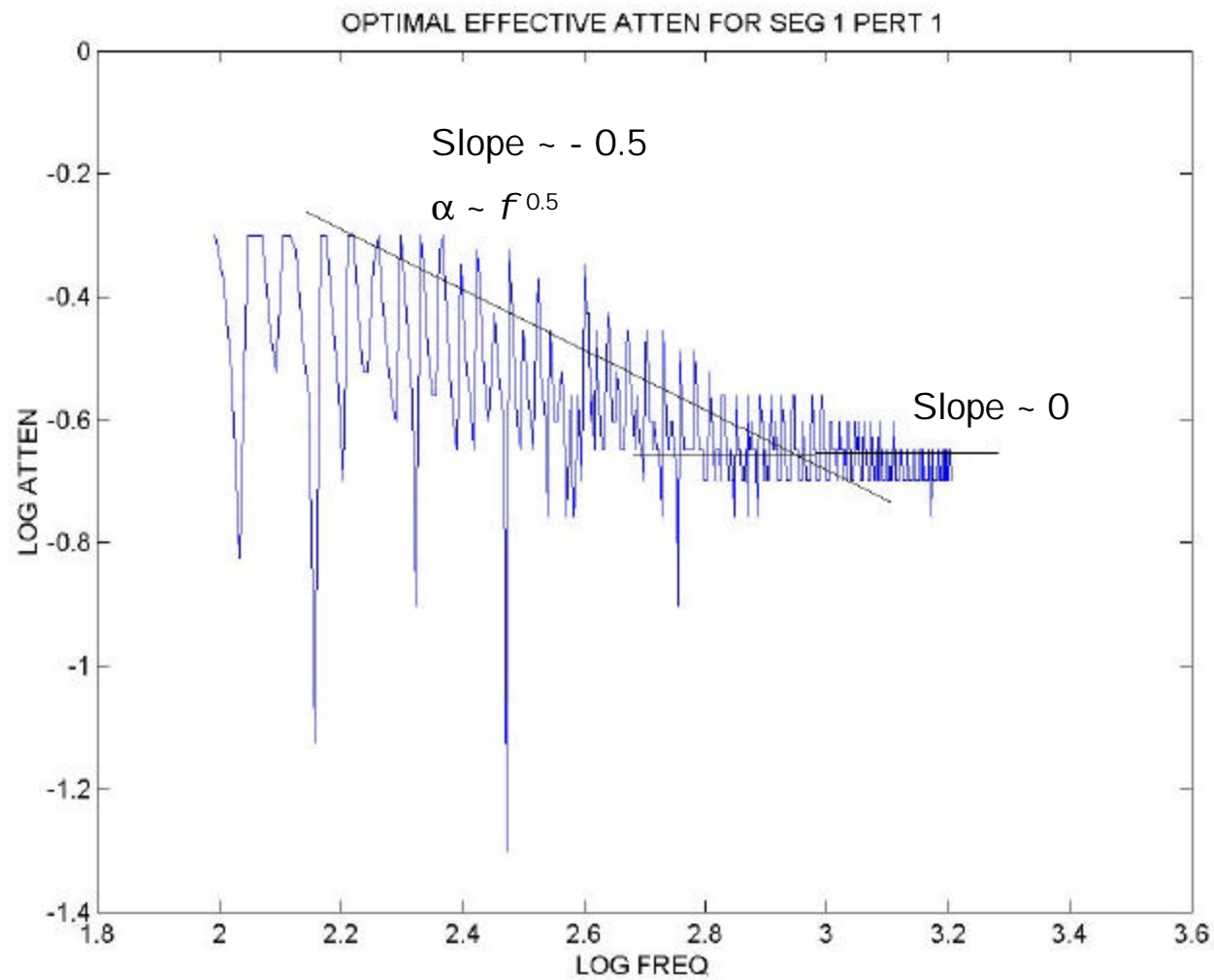
# Environment 1



# Results, Environment 1

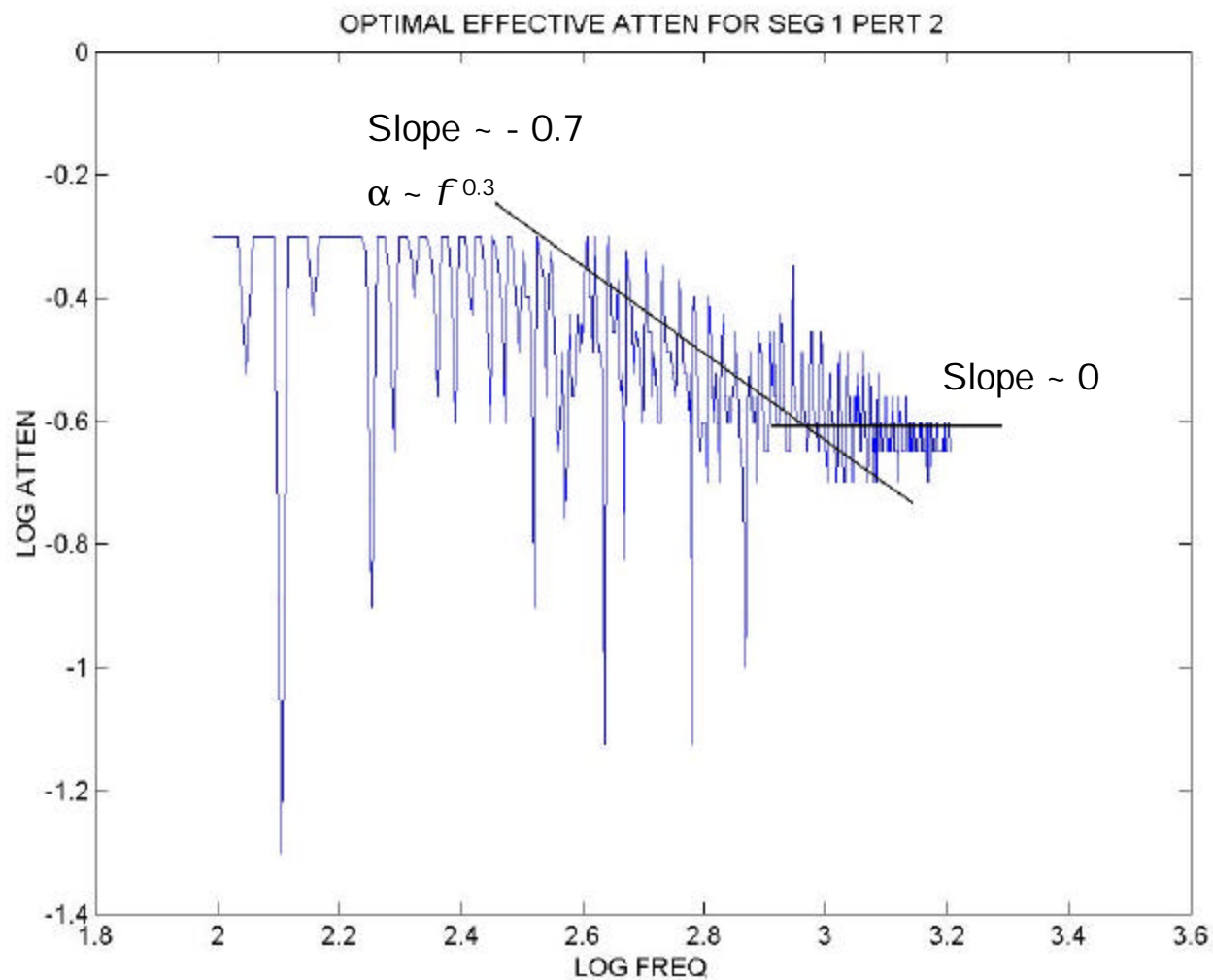


# Log-log analysis of Env 1, Pert 1

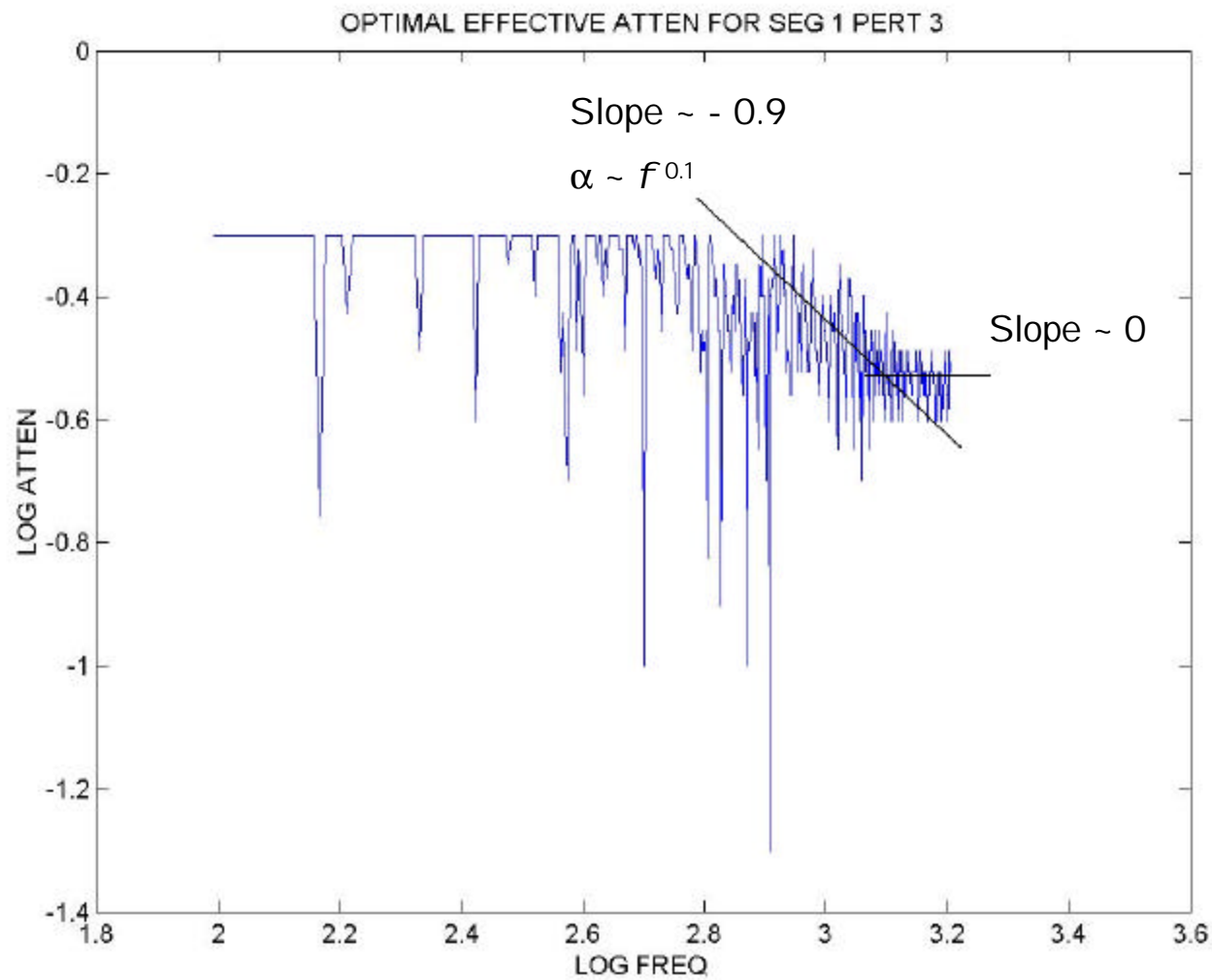




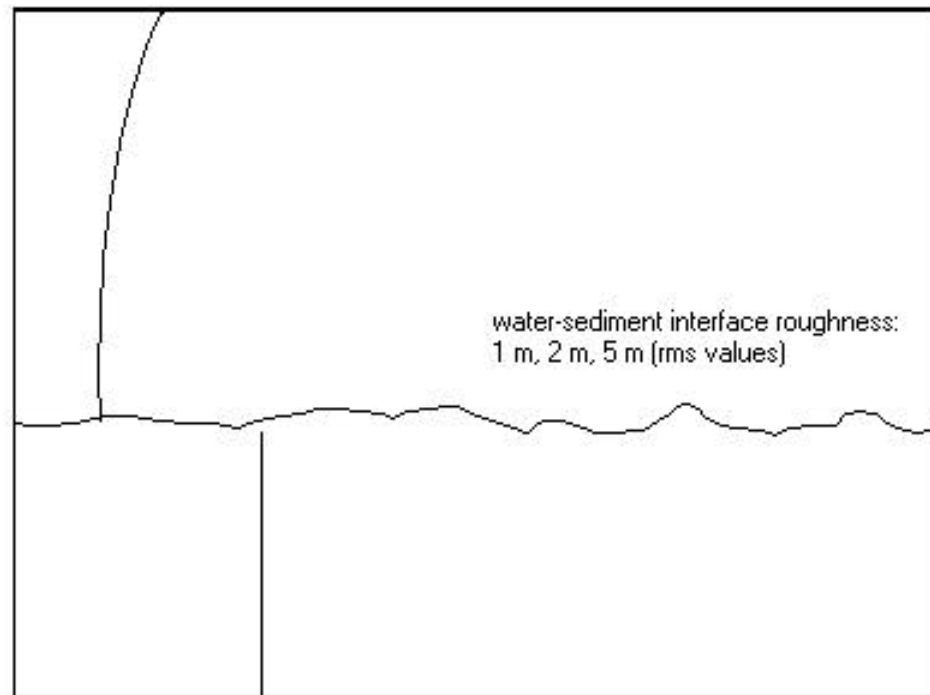
# Log-log analysis of Env 1, Pert 2



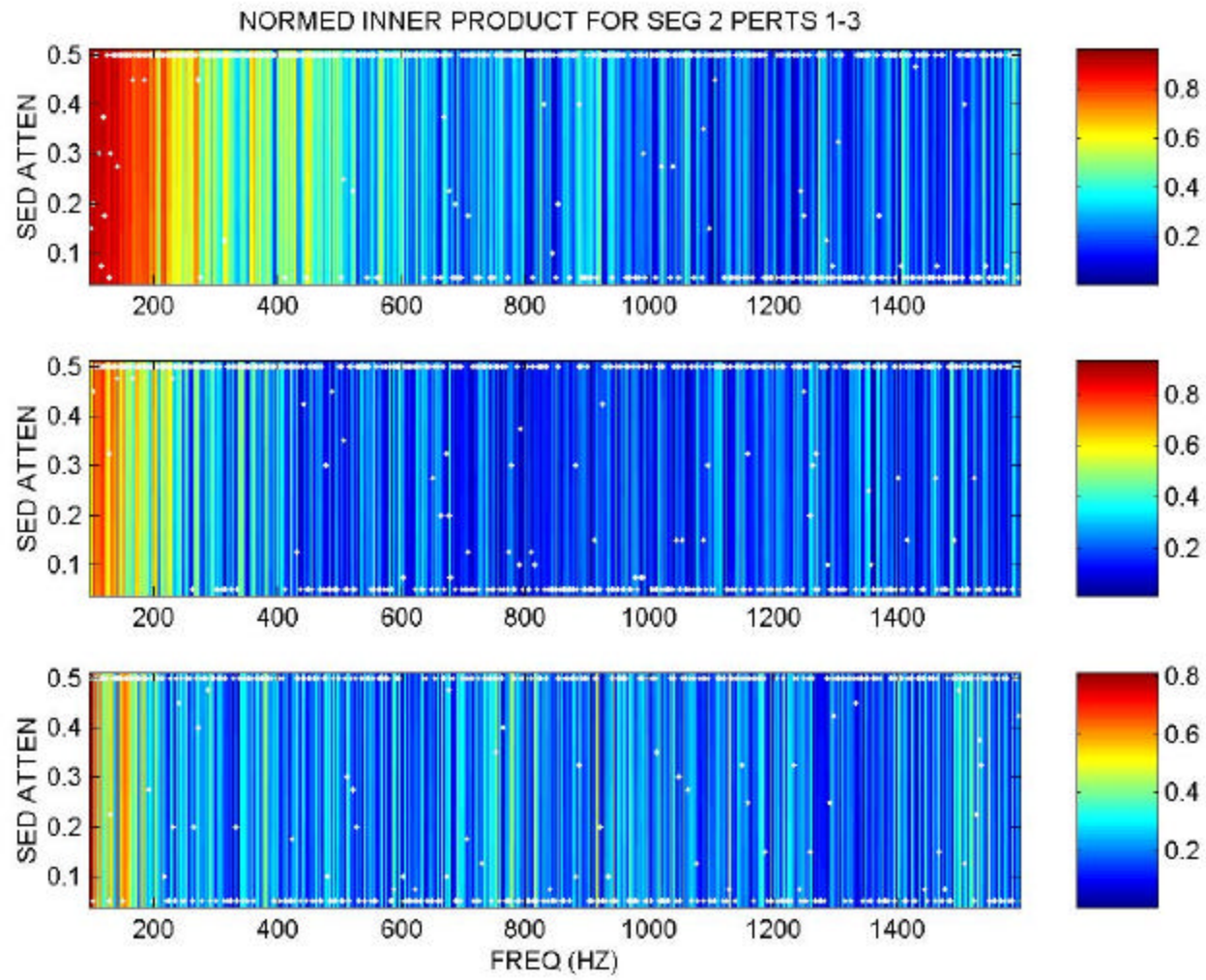
# Log-log analysis of Env 1, Pert 3



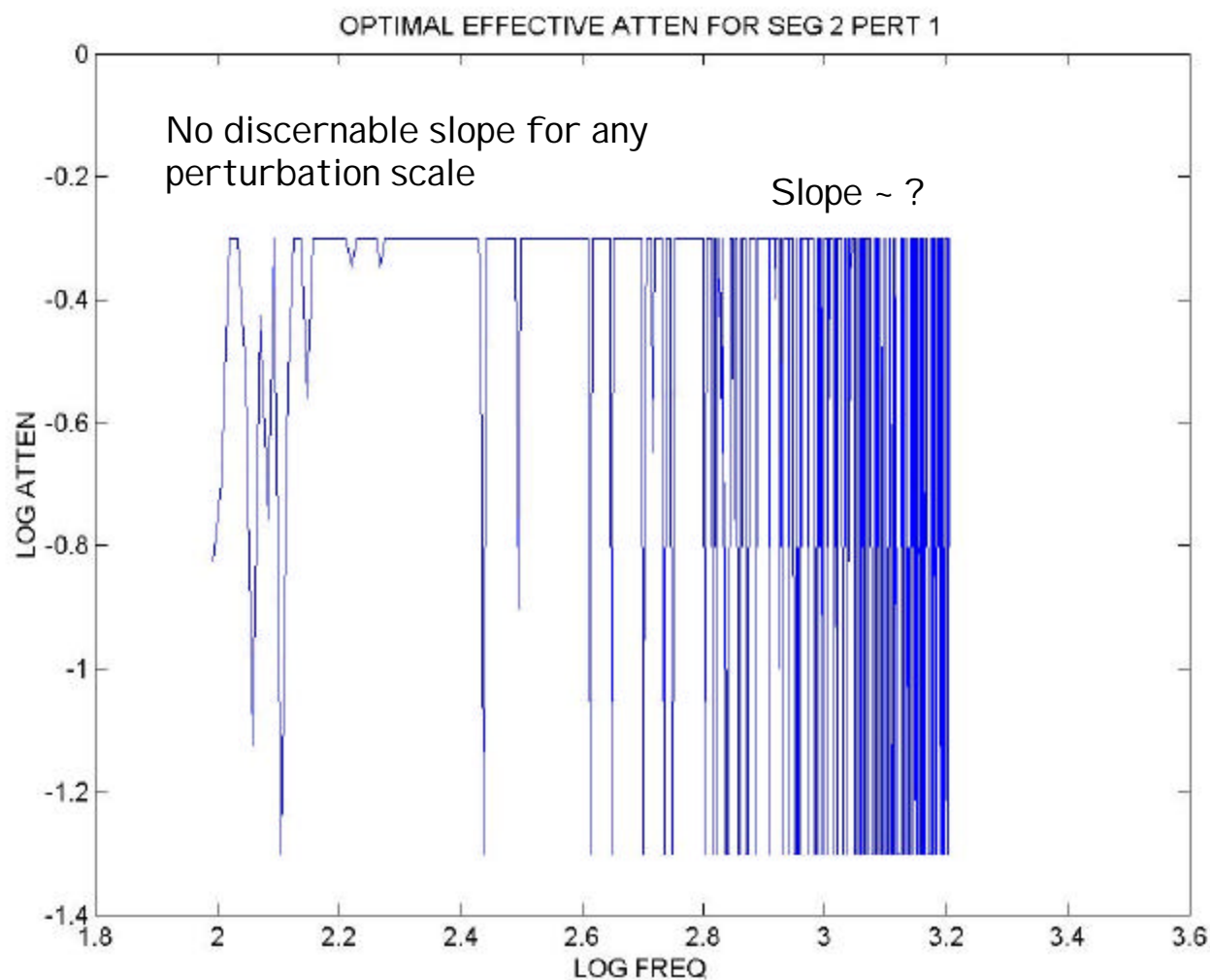
## Environment 2



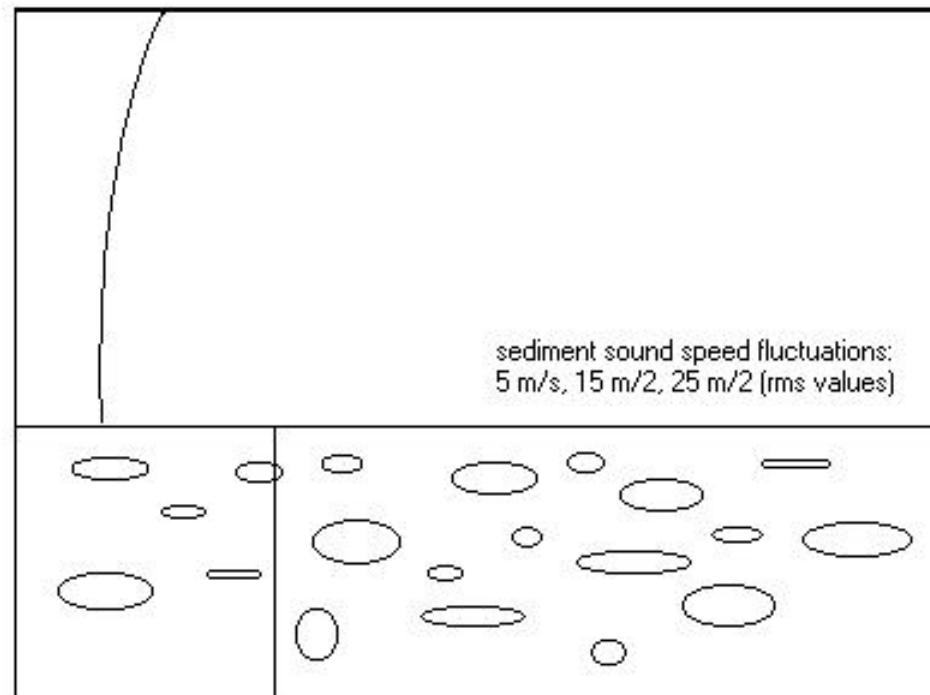
## Results, Environment 2



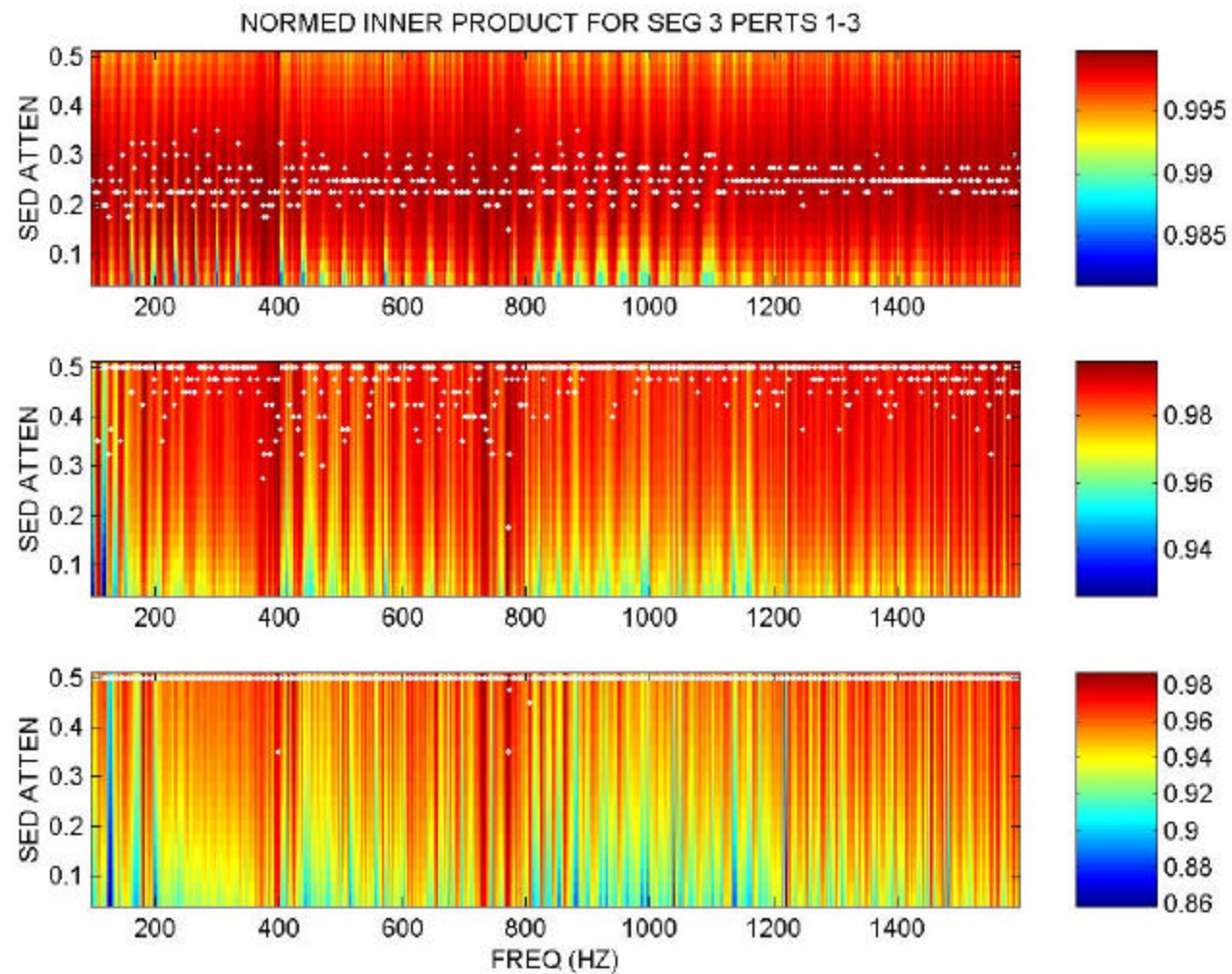
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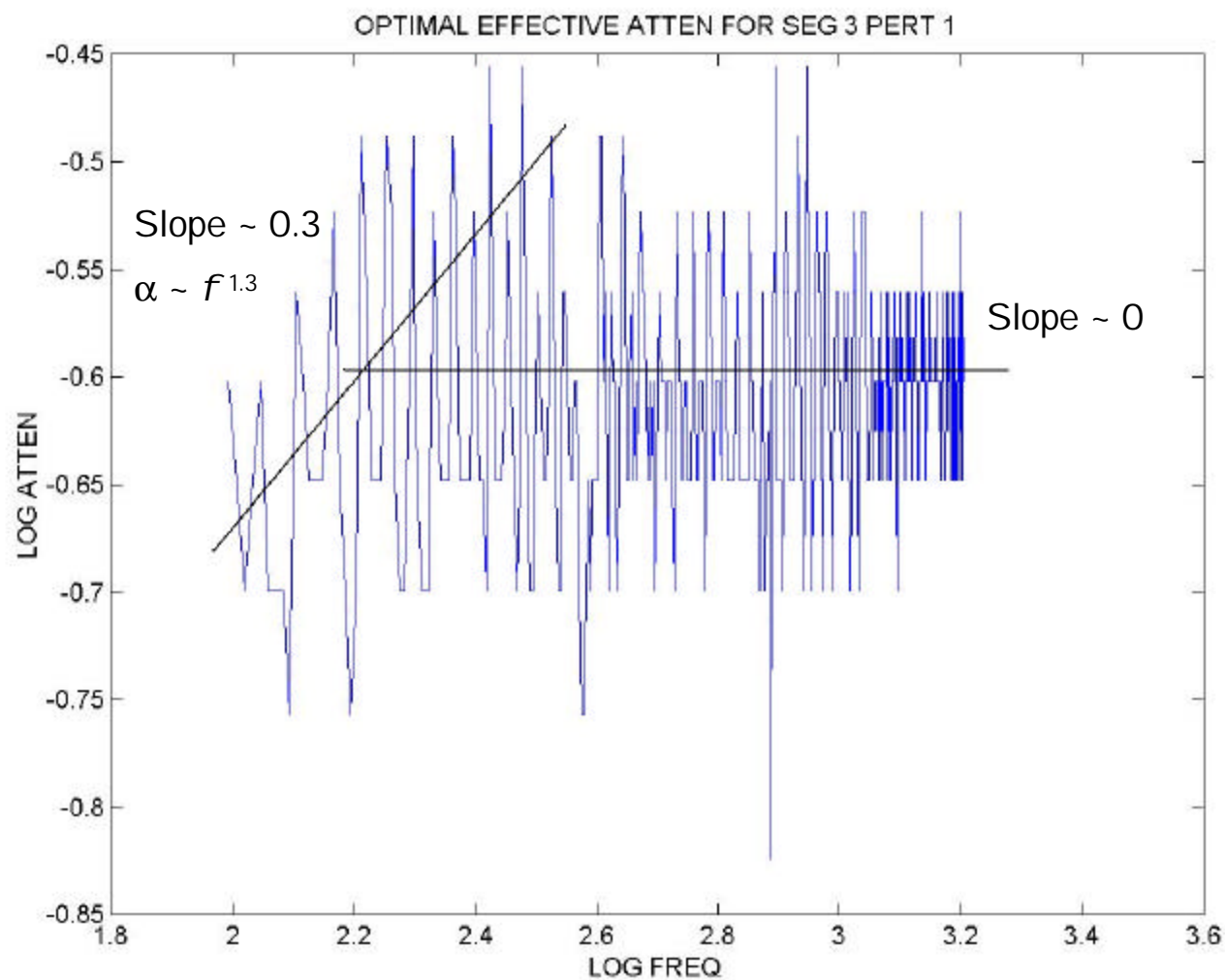
# Environment 3



# Results, Environment 3

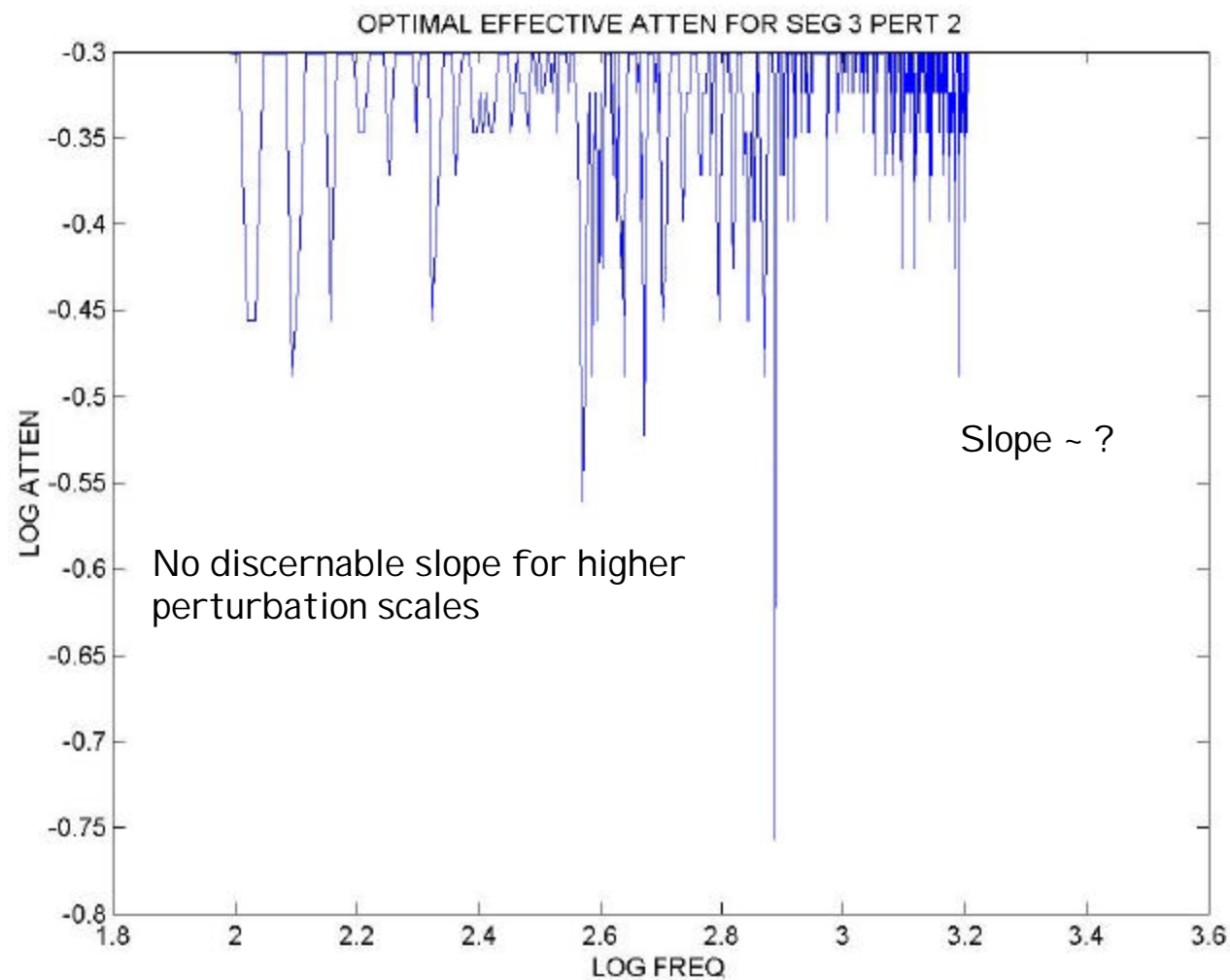


# Log-log analysis of Env 3, Pert 1

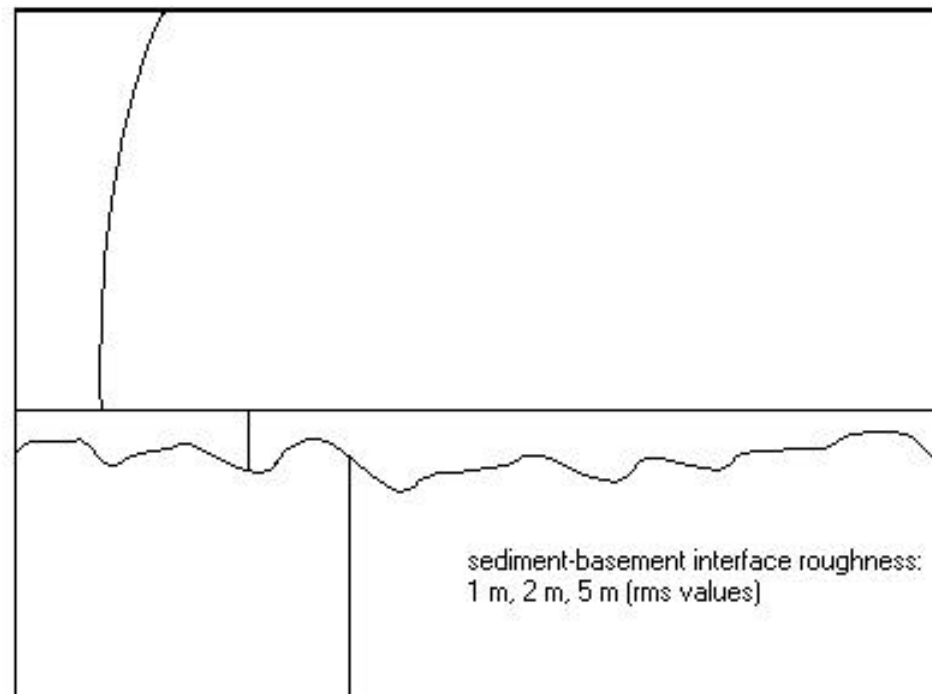




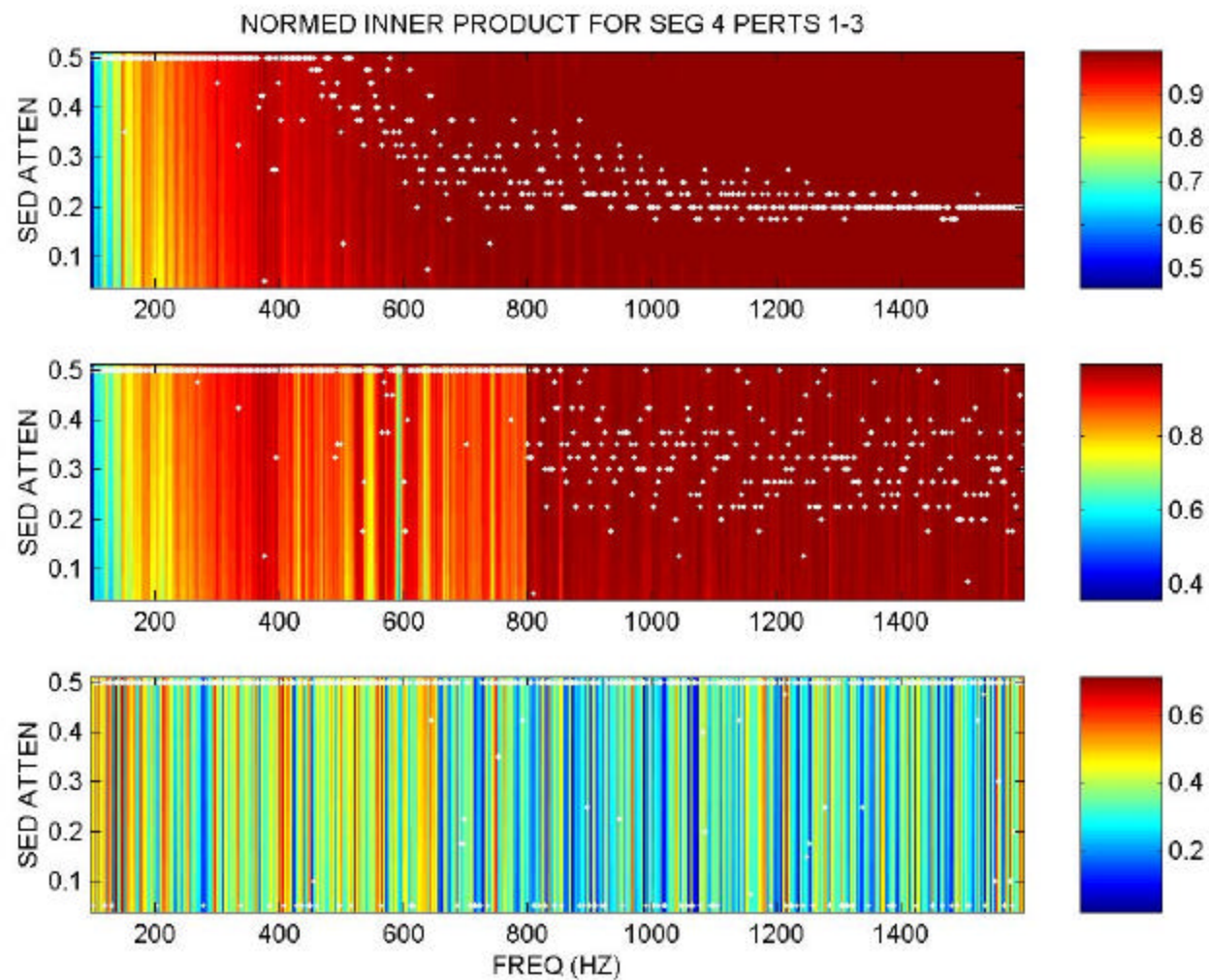
## Log-log analysis of Env 3, Pert 2



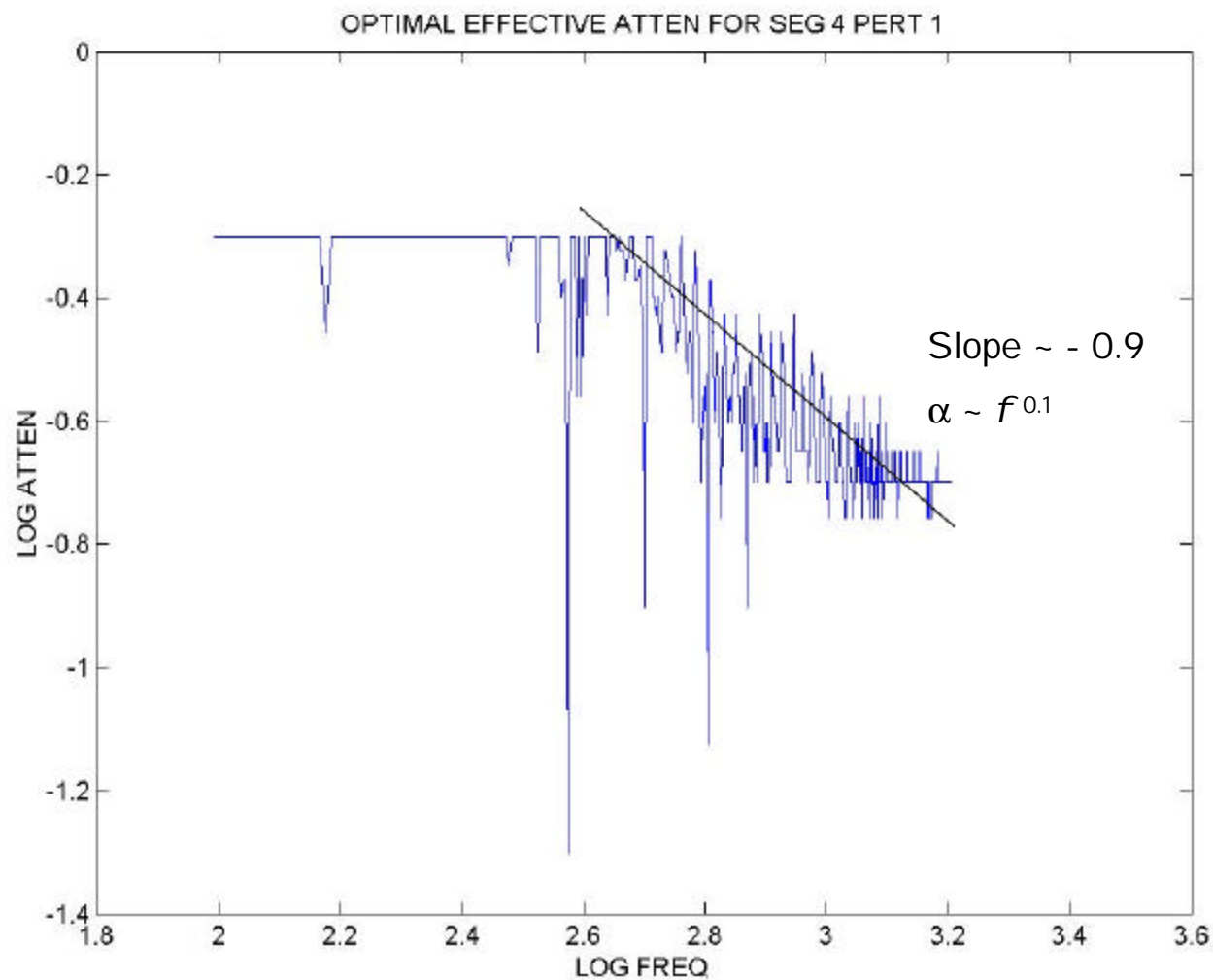
# Environment 4



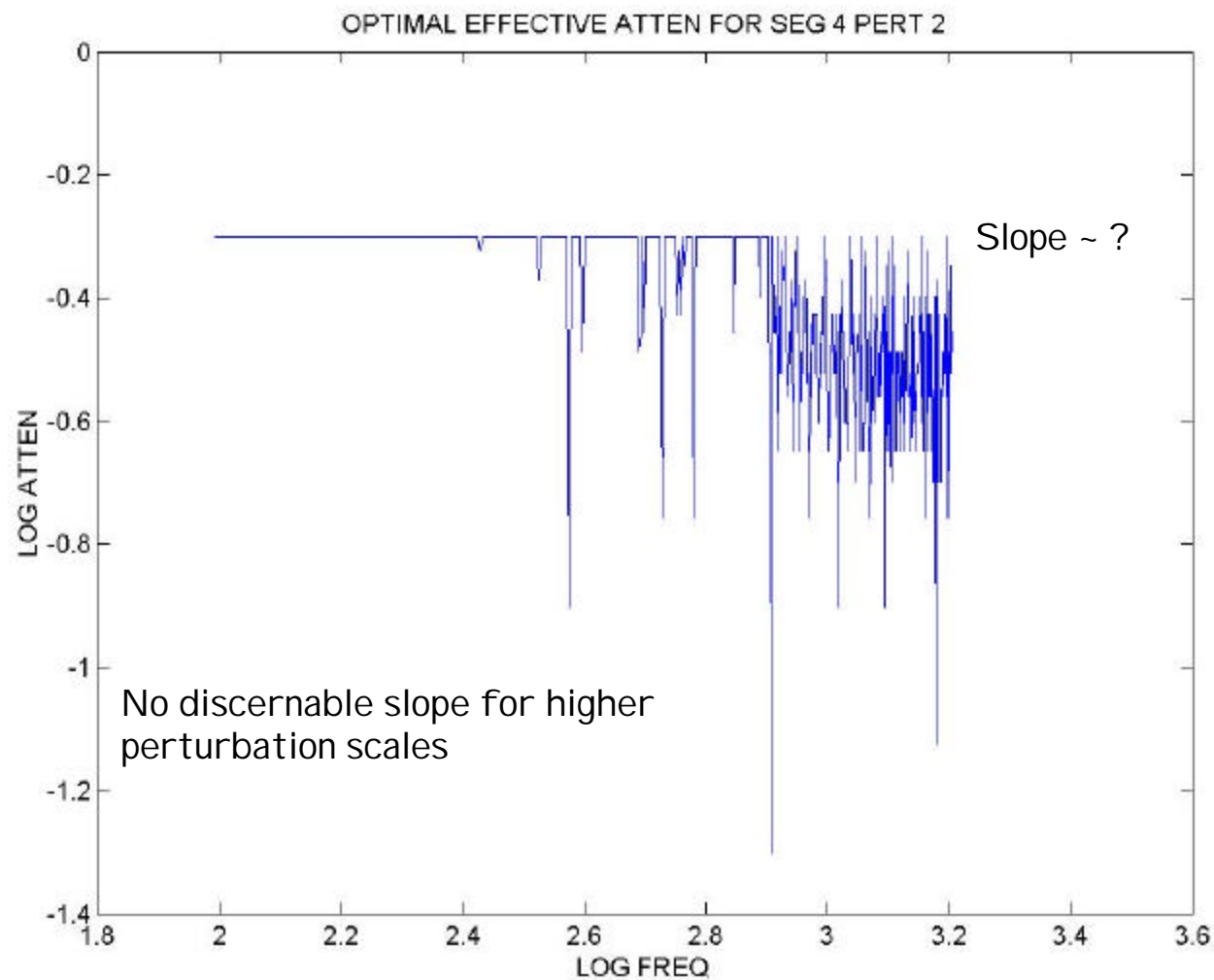
# Results, Environment 4



# Log-log analysis of Env 4, Pert 1



## Log-log analysis of Env 4, Pert 2

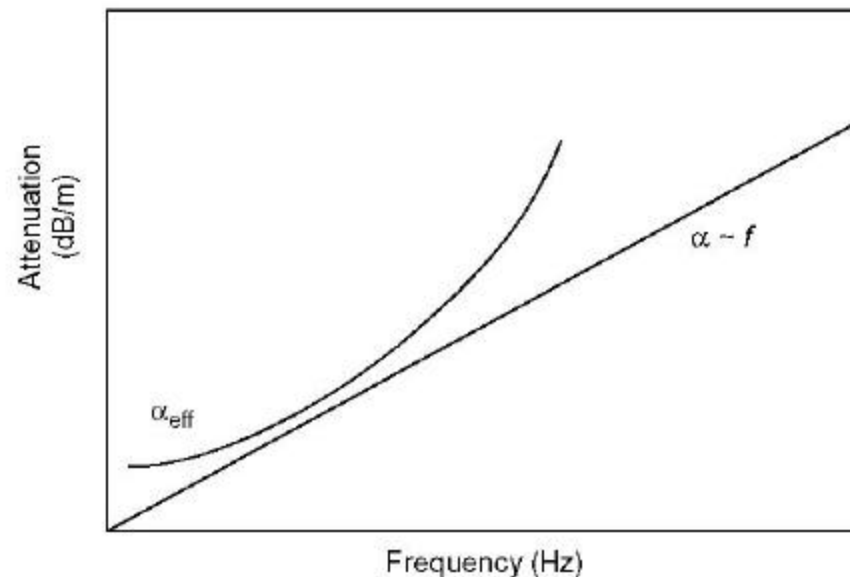


# Summary – Part I

- Environmental fluctuations can have significant impact on inversion of sediment attenuation.
- Water-sediment interface roughness seemed to create largest variability in effective attenuation. No trend observed over bandwidth.
- Sediment sound speed gradients and sediment-basement roughness both seemed to introduce noticeable trend in frequency dependence at larger ranges. Specifically, there was enhanced attenuation at the lower frequencies with values of  $x$  typically  $-0.5$  to  $-0.9$  (i.e.,  $\alpha \sim f^{0.1}$  to  $\alpha \sim f^{0.5}$ ) over the band  $f = 100 - 500$  Hz.
- These results imply higher loss per wavelength at lower frequencies, or even nearly constant loss per distance over band.

# Summary – Part I

- Cause may be primary loss mechanism in these cases due to sub-sediment/basement effects. Thus, lower frequencies interact more readily, thereby increasing the effective attenuation.
- This suggests environments with  $x > 1$  may be due to water/sediment interface, or near interface, influences. Potential causes could be small-scale roughness/scattering or even near bottom biologics. Longer range effects could even be related to rough surface scattering.
- If higher frequencies incur enhanced scattering, may expect frequency dependence of attenuation of the form



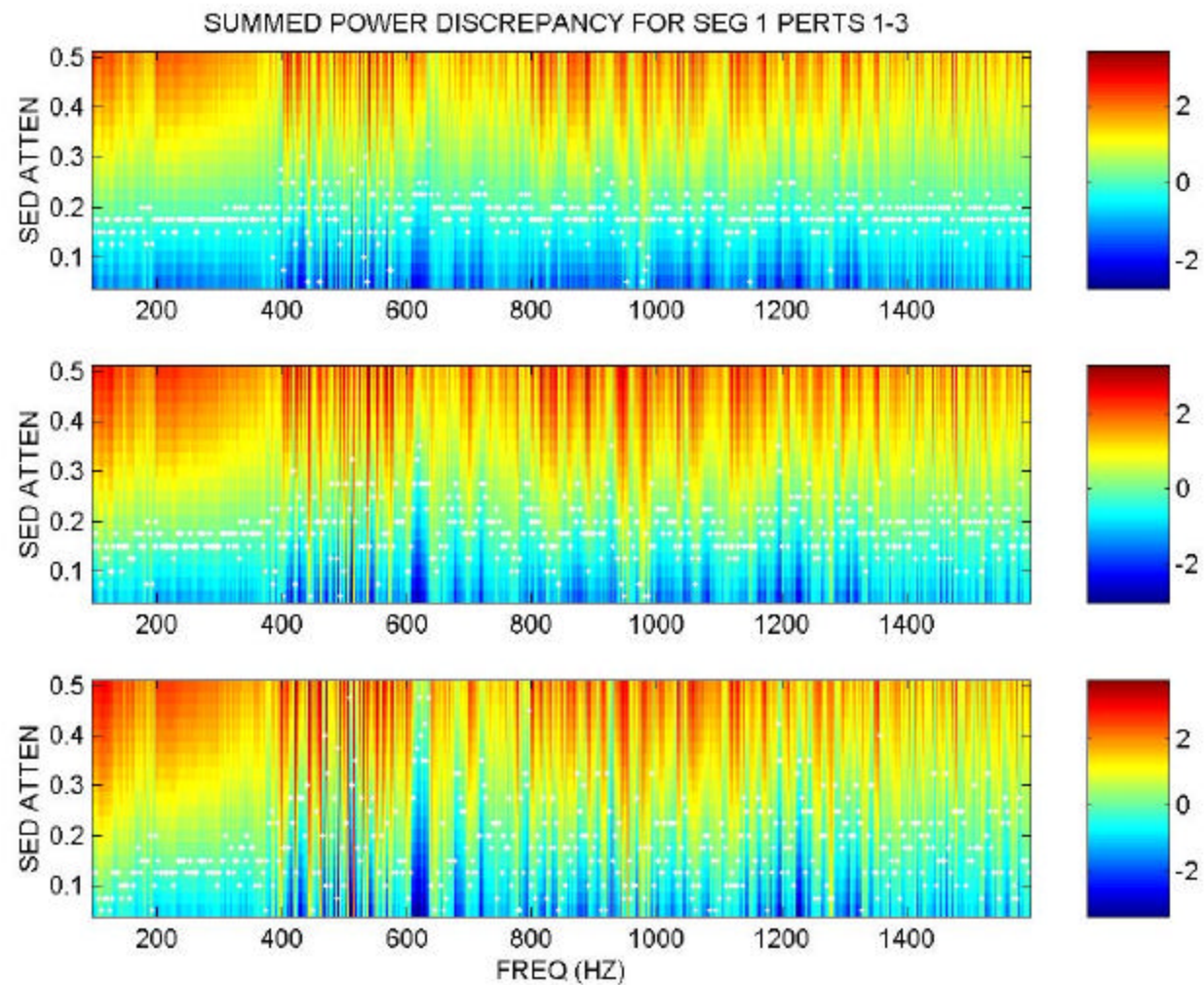
# Approach – Part II , New Cost Function

- Previous cost function based on incoherent correlation over depth. However, no reason to expect correlation between scattered field structure (e.g., from rough interface) and range-independent field with effective attenuation.
- Instead, choose simple comparison of total energy integrated over depth, i.e.

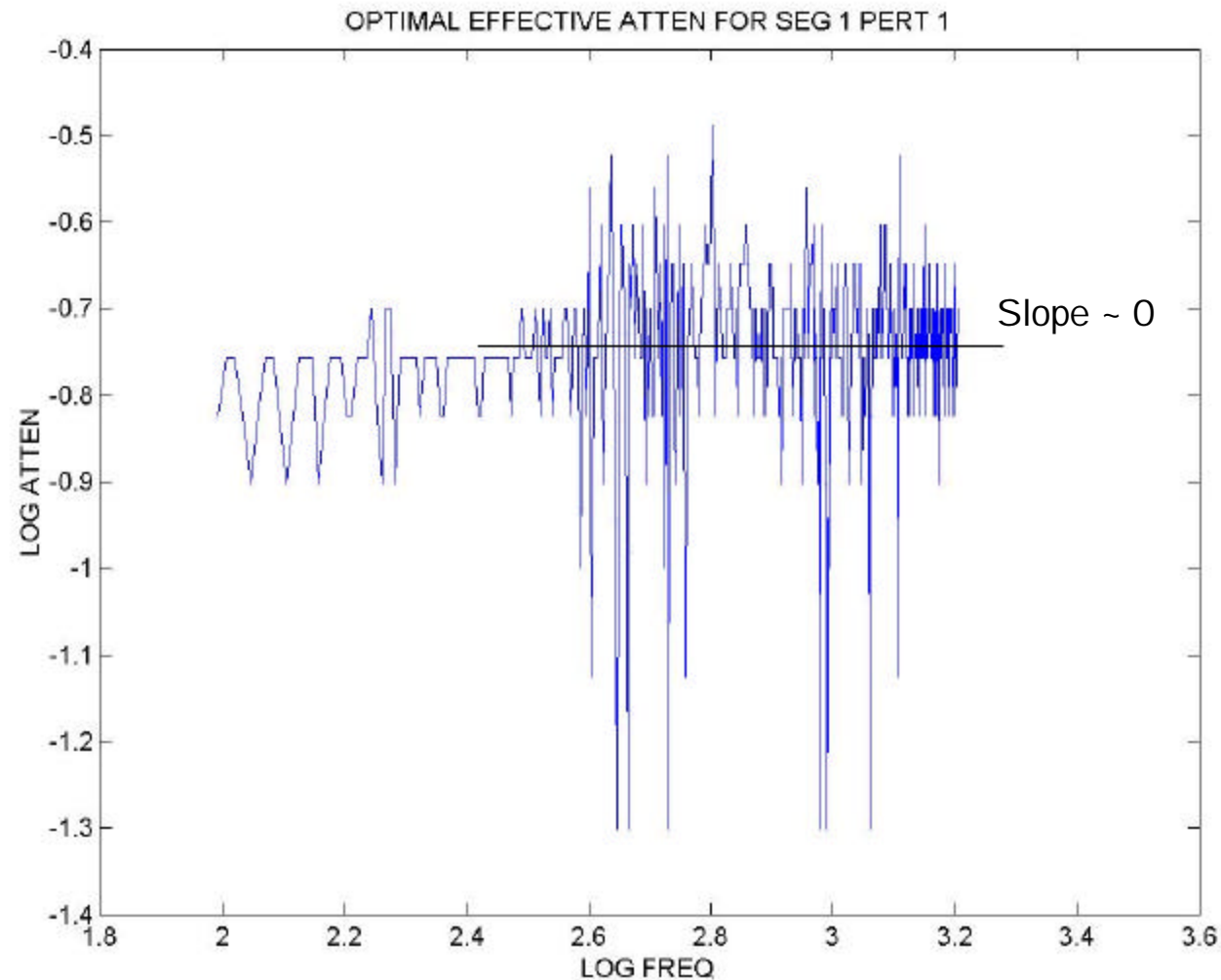
$$C(r, f, b) = \sum_j \left| p(r, z_j) \right|^2 - \sum_j \left| p'_b(r, z_j) \right|^2$$



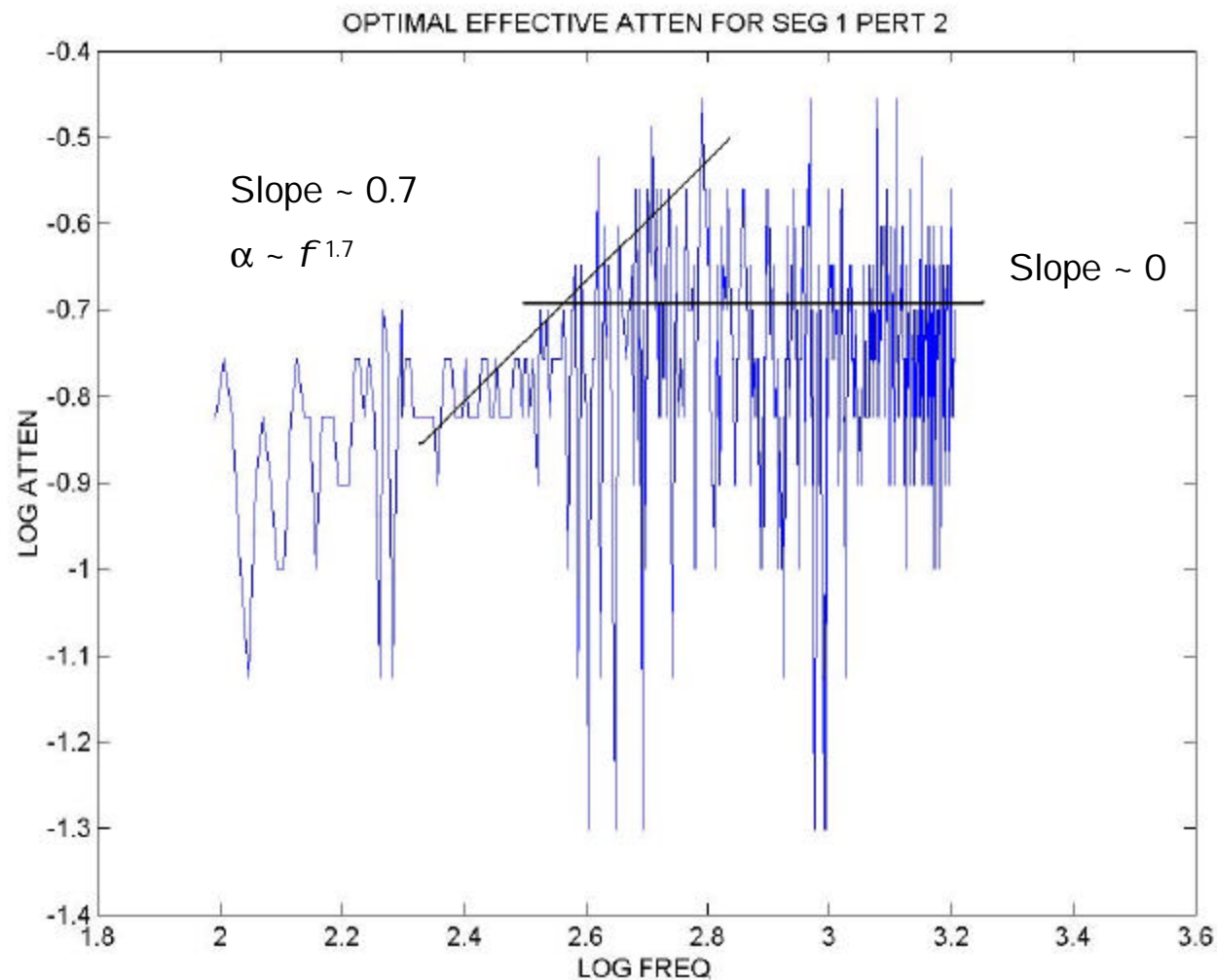
# Results, Environment 1



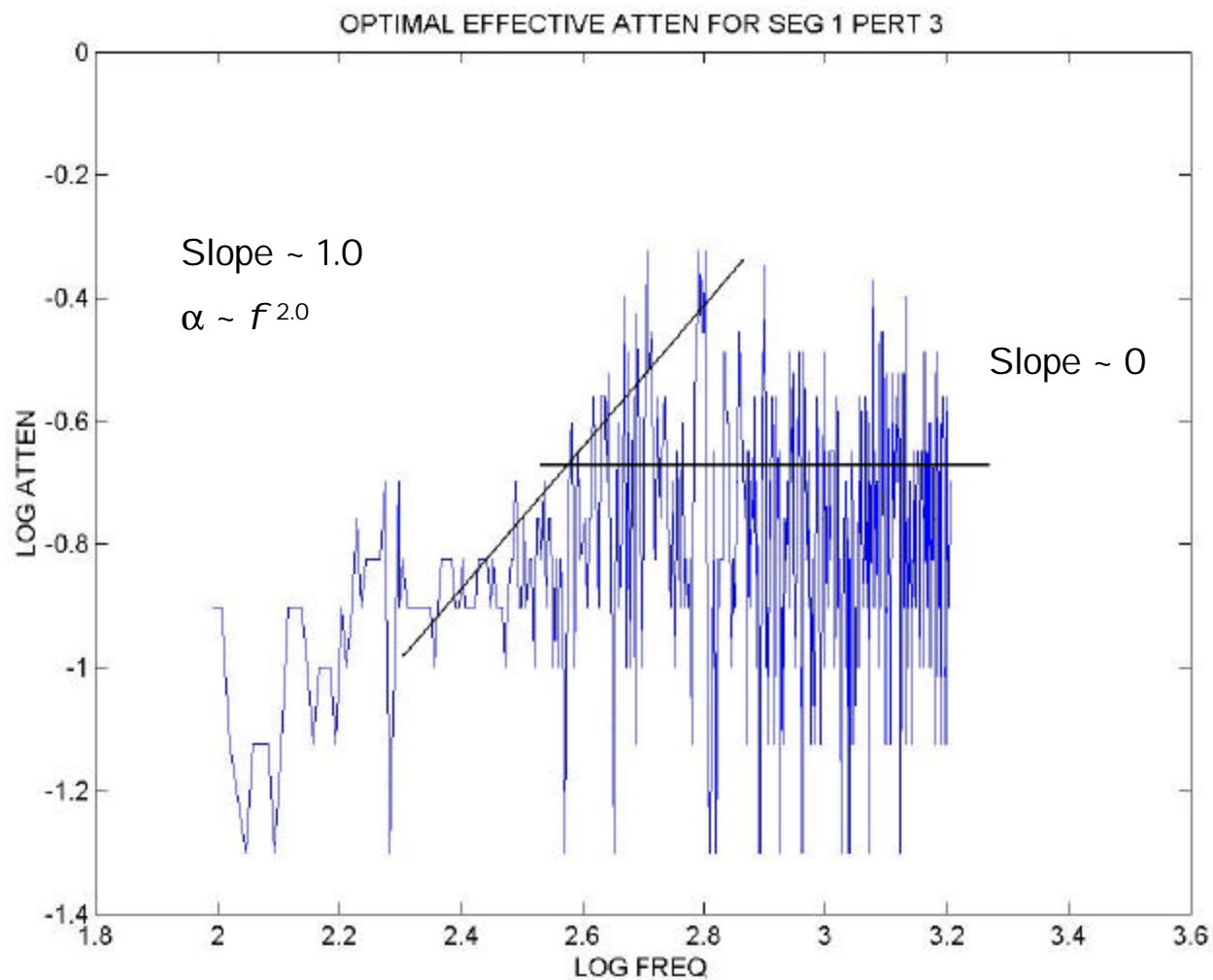
# Log-log analysis of Env 1, Pert 1



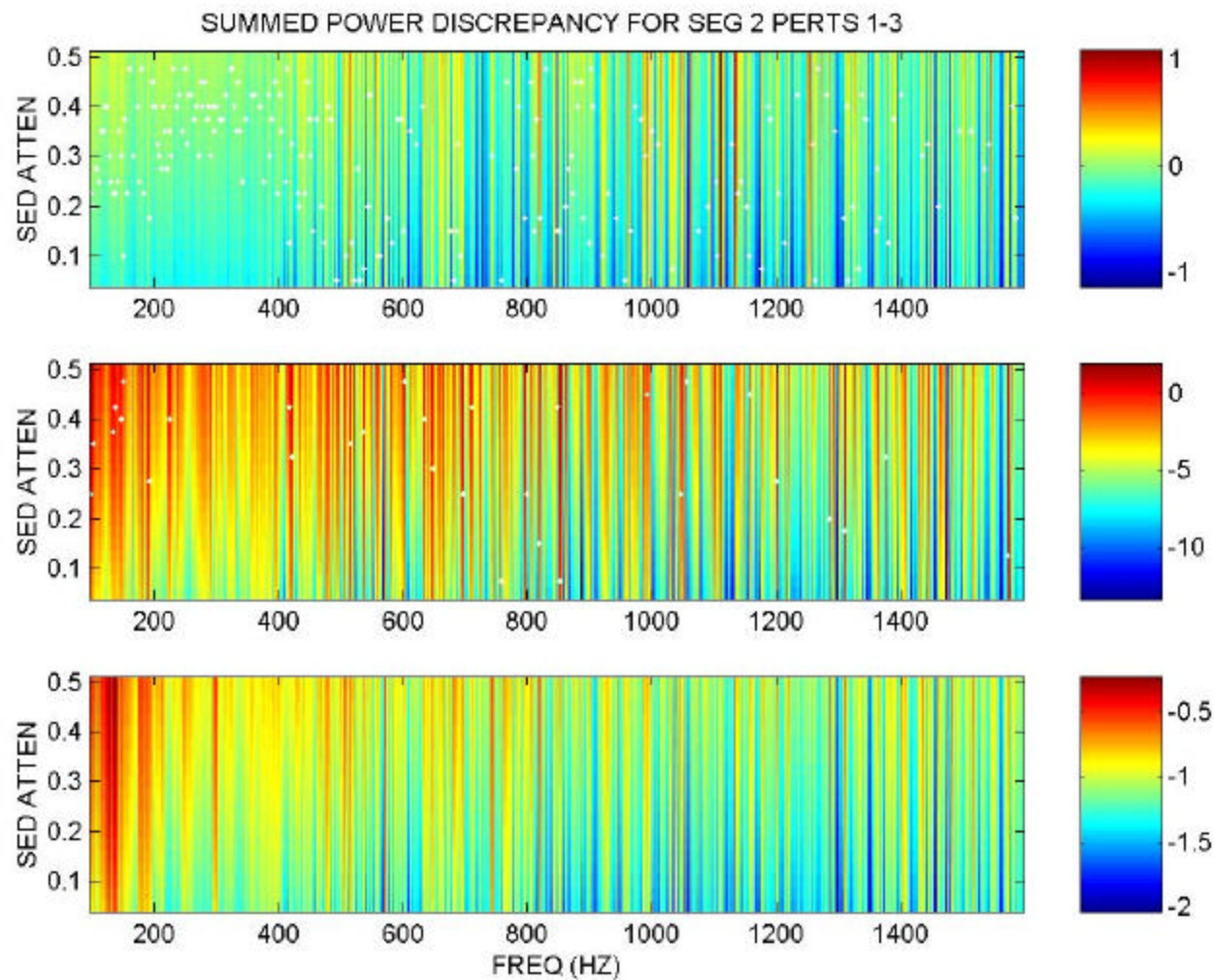
## Log-log analysis of Env 1, Pert 2



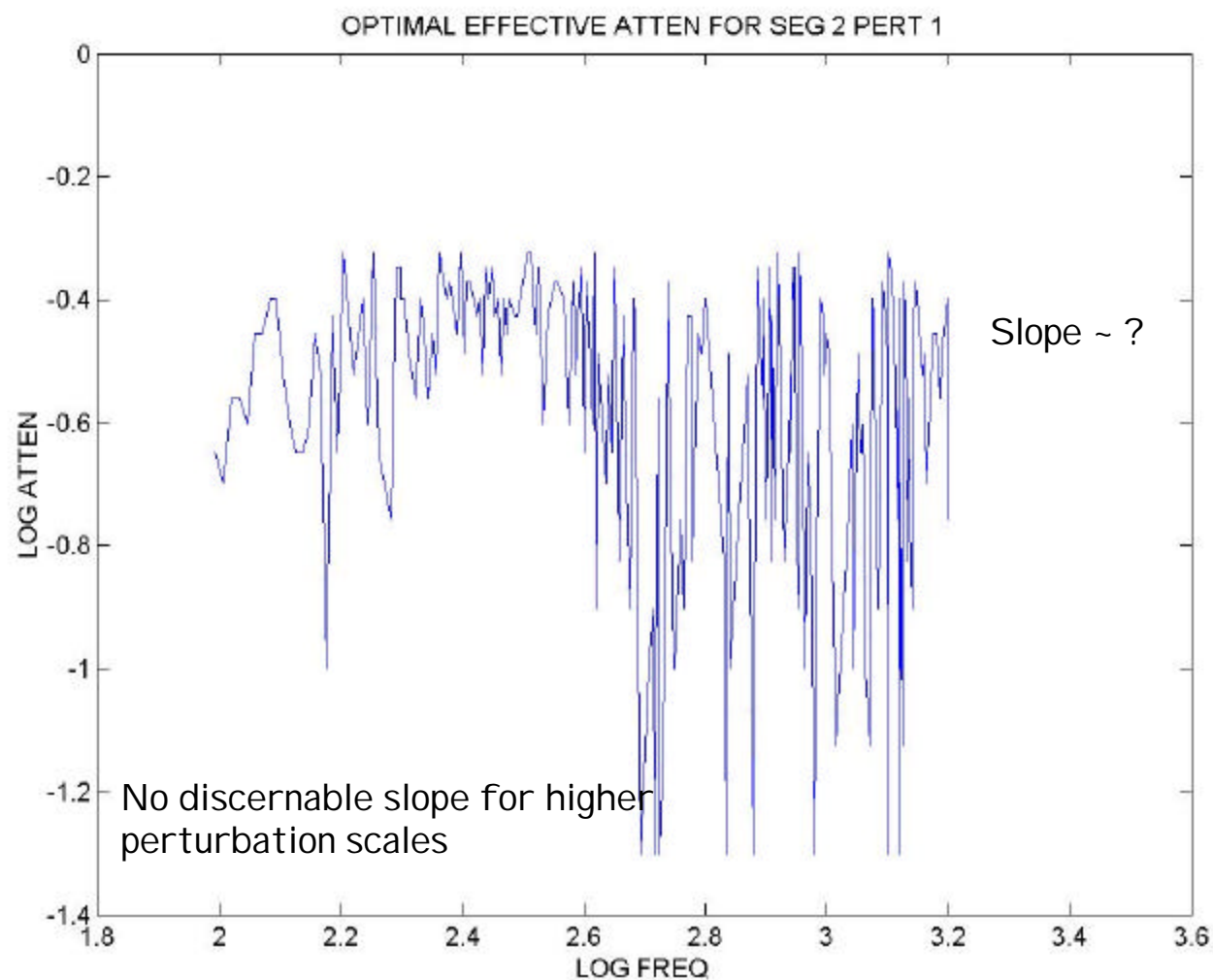
# Log-log analysis of Env 1, Pert 3



## Results, Environment 2

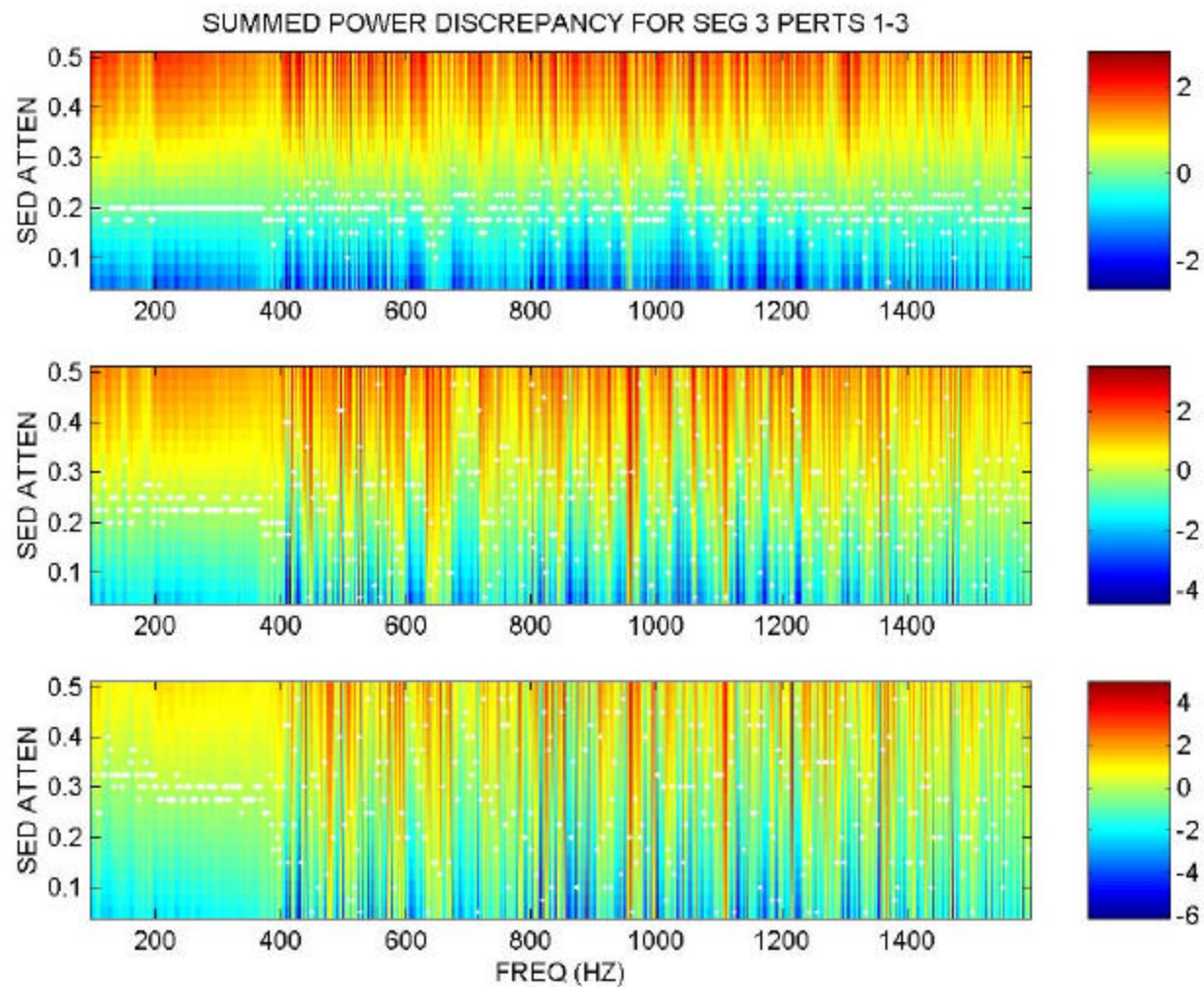


# Log-log analysis of Env 2, Pert 1

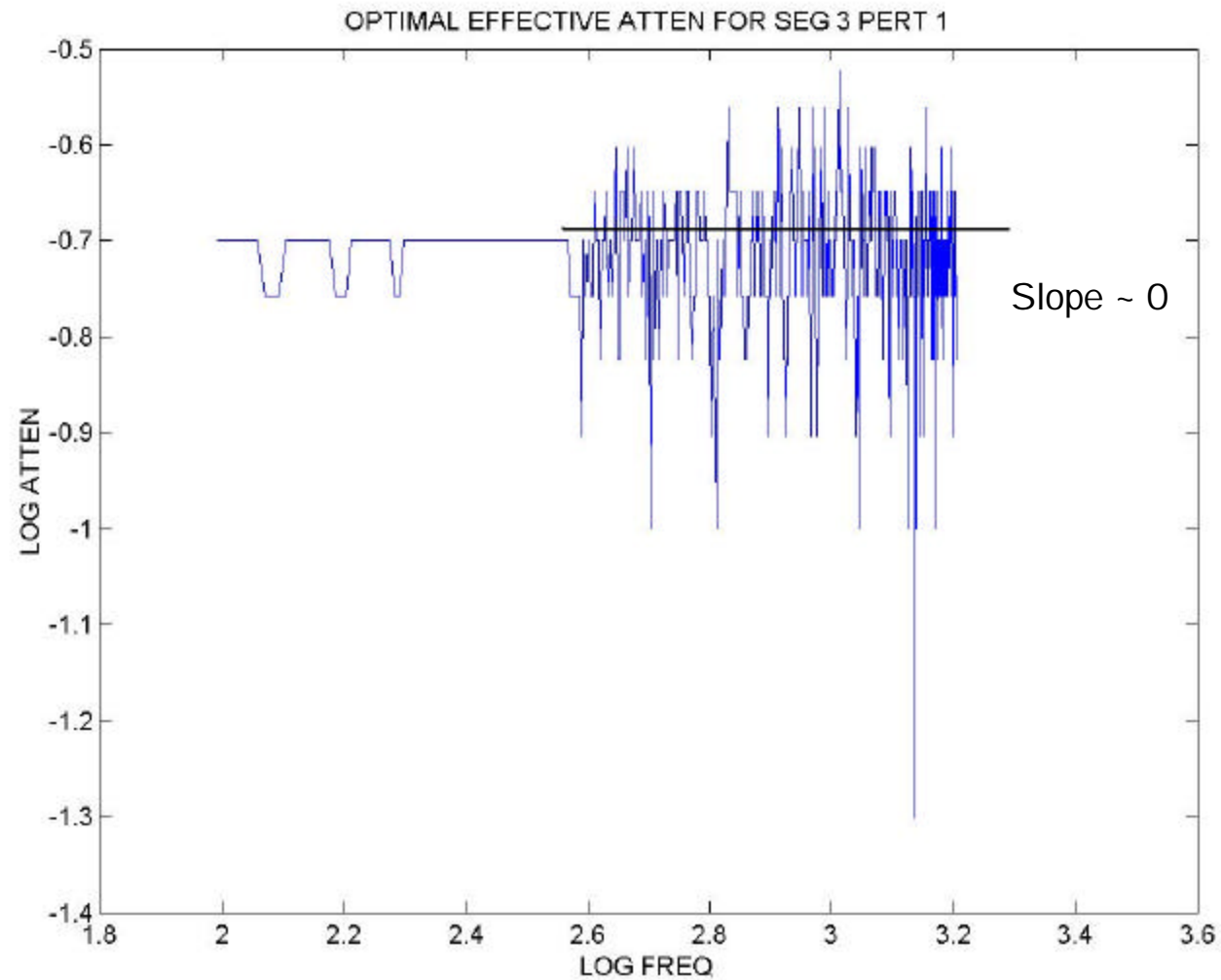




# Results, Environment 3

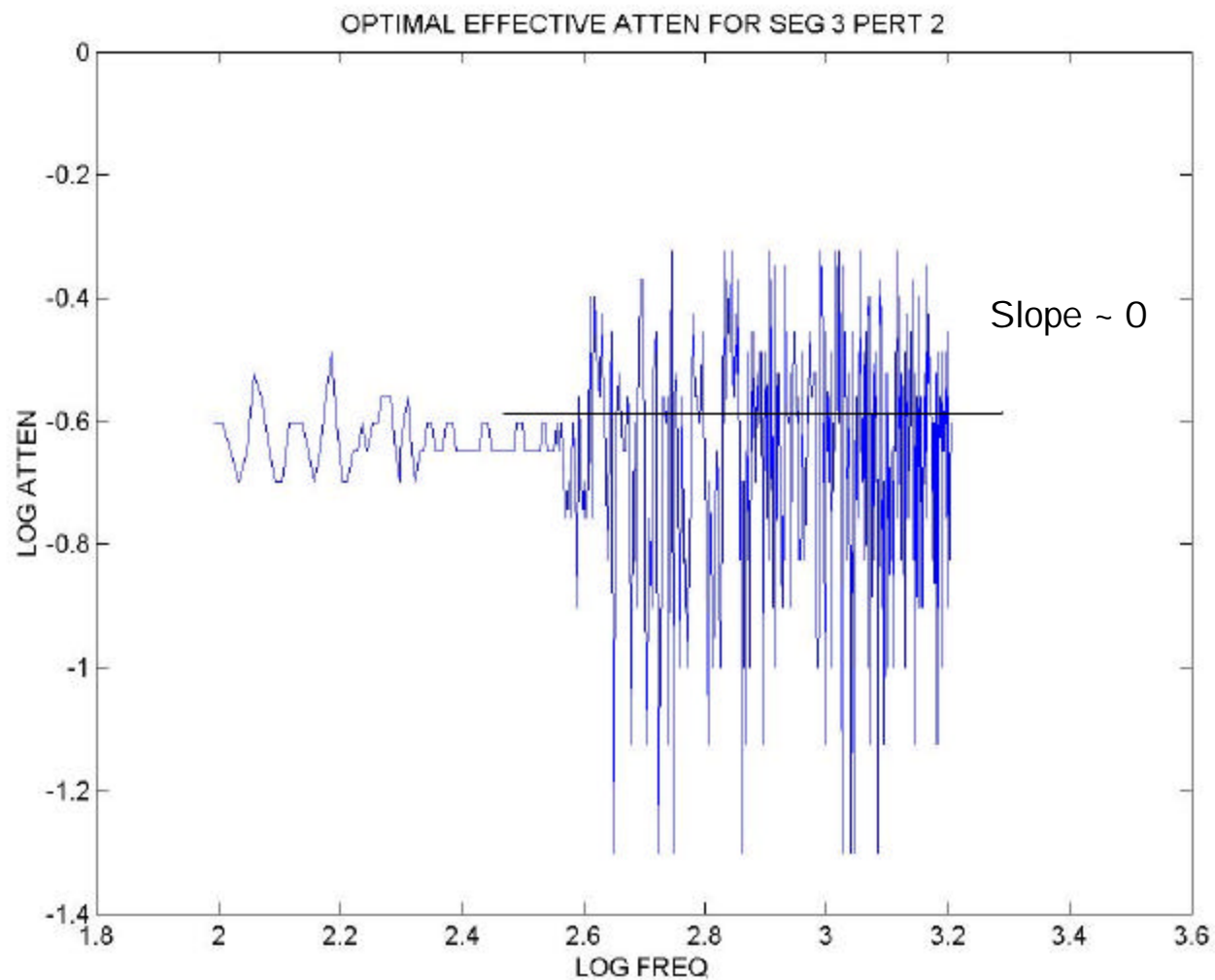


# Log-log analysis of Env 3, Pert 1

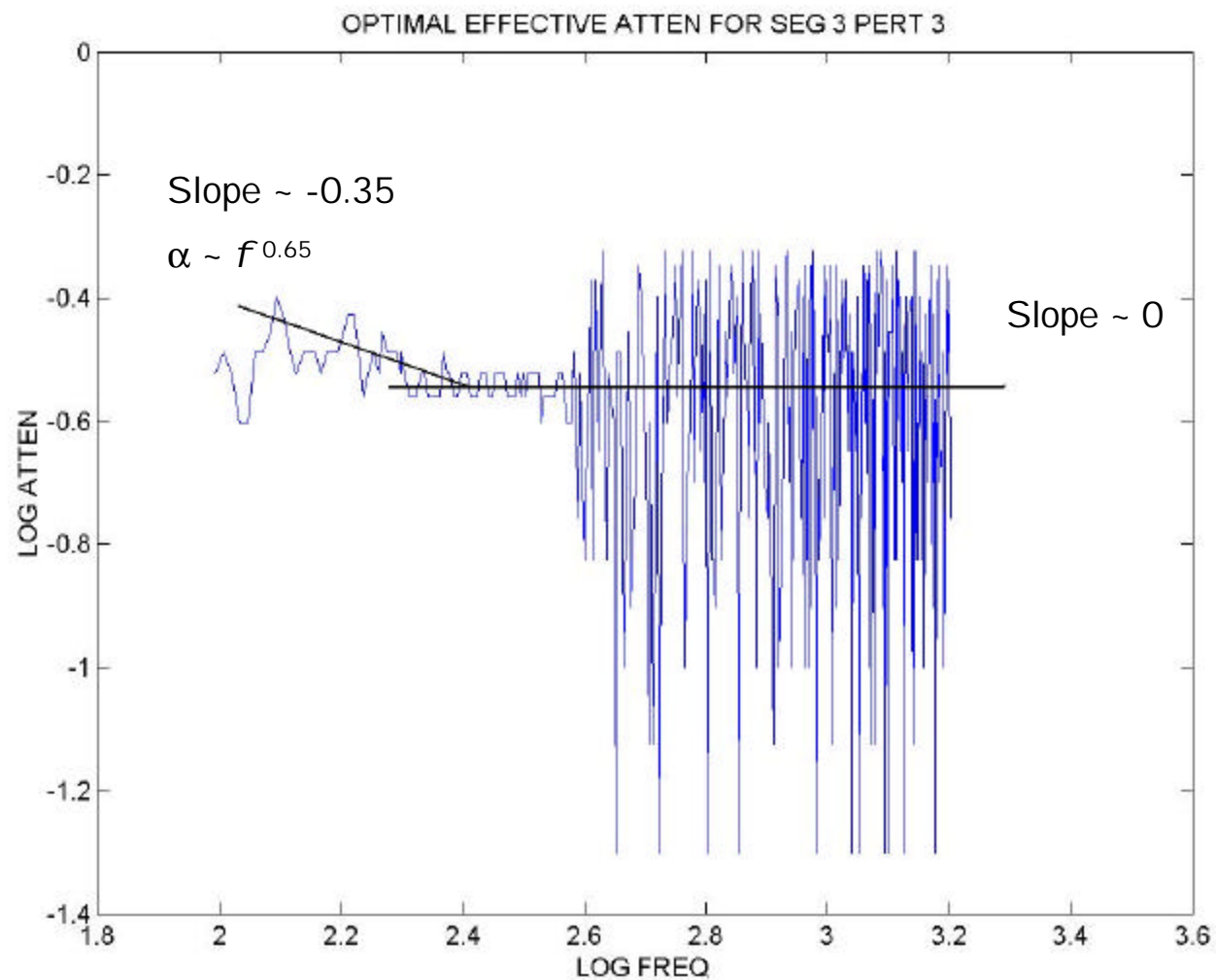




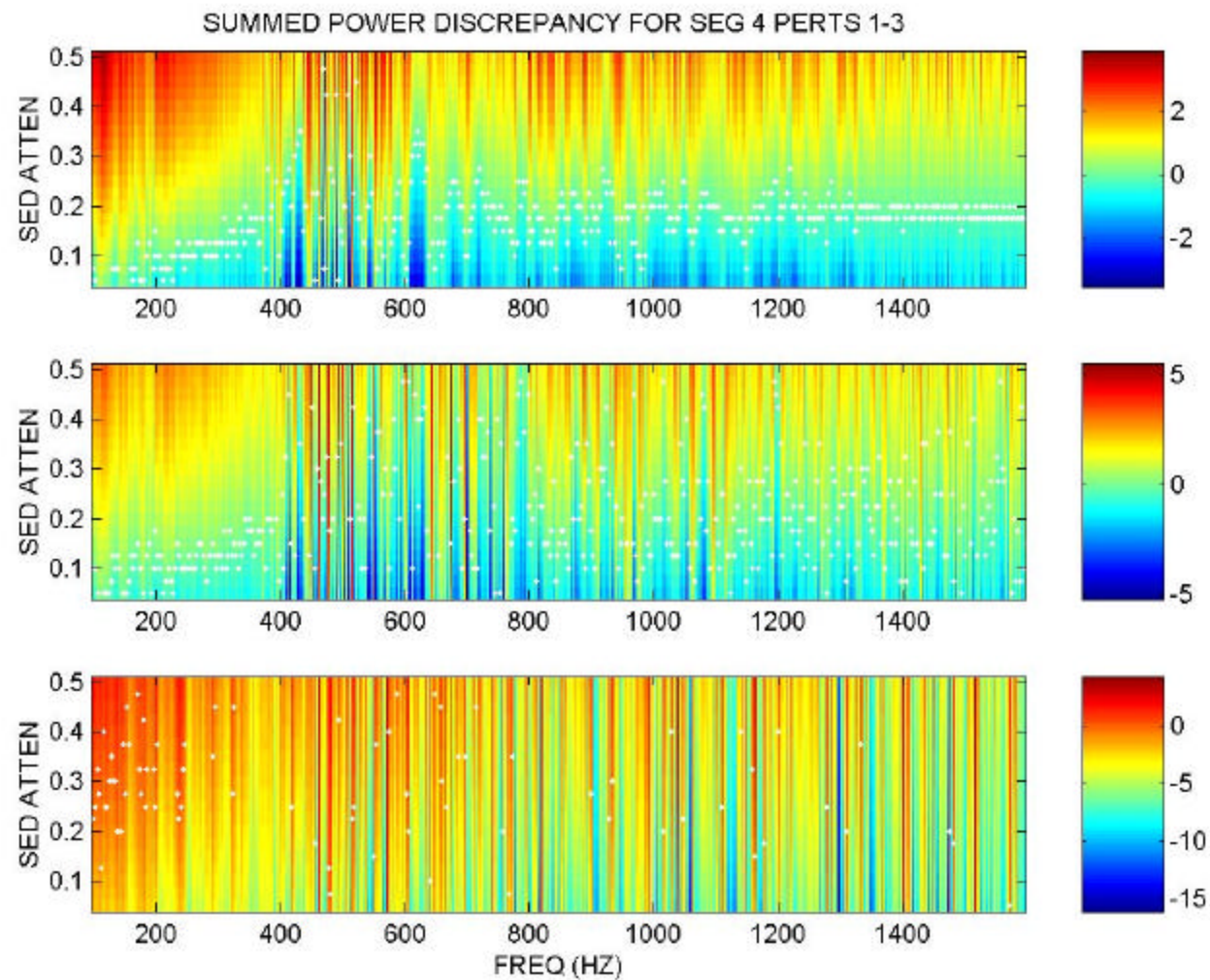
## Log-log analysis of Env 3, Pert 2



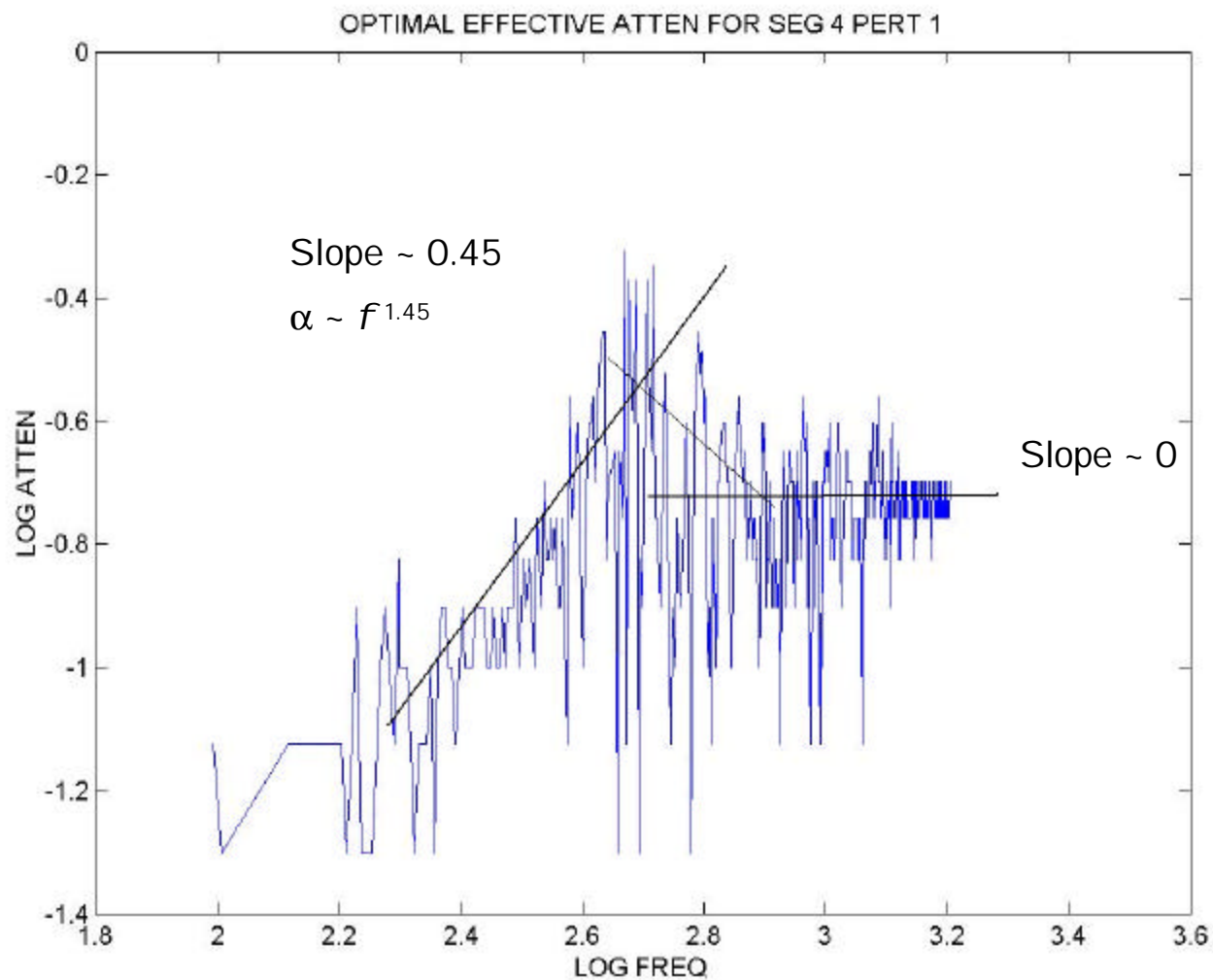
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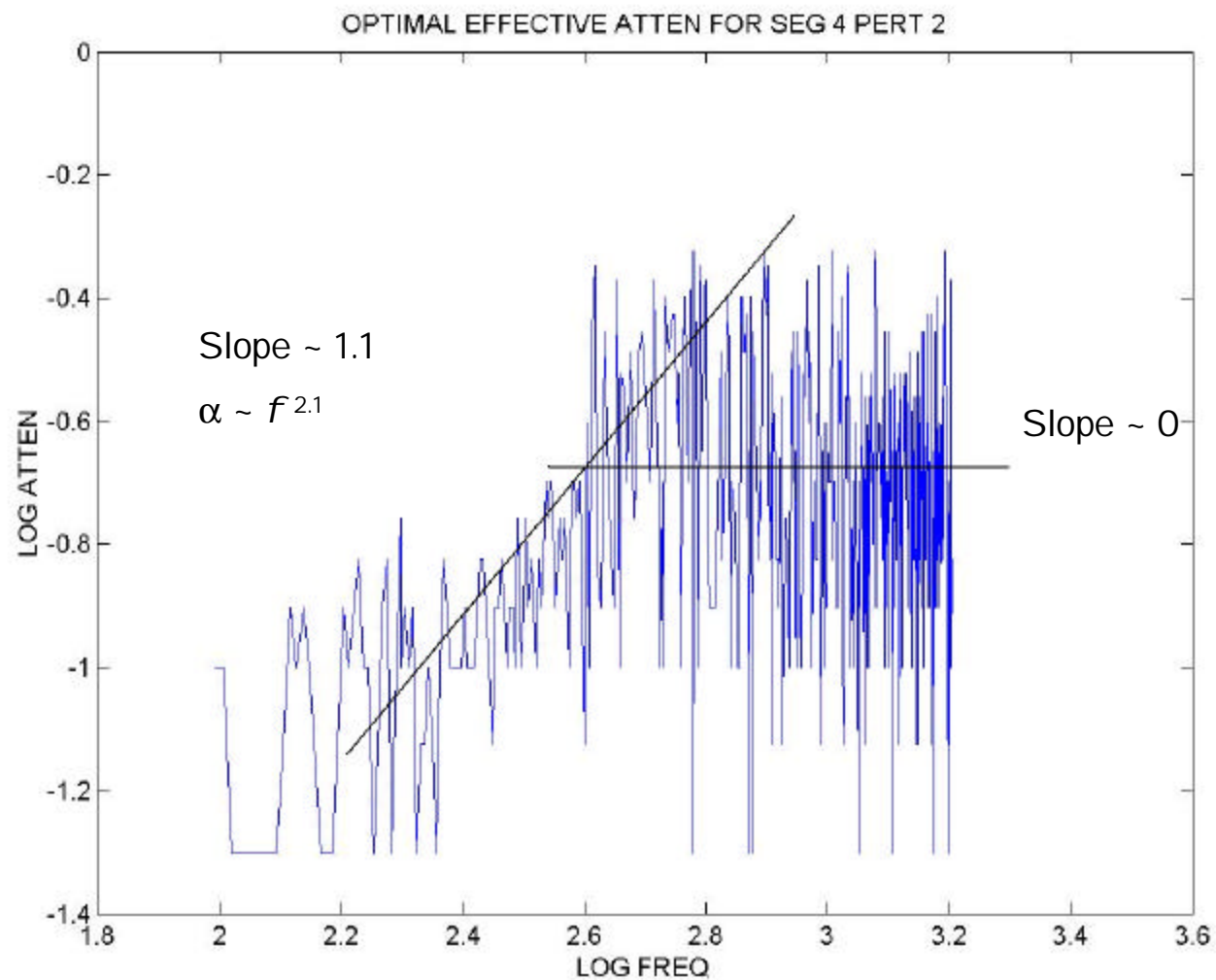
# Results, Environment 4



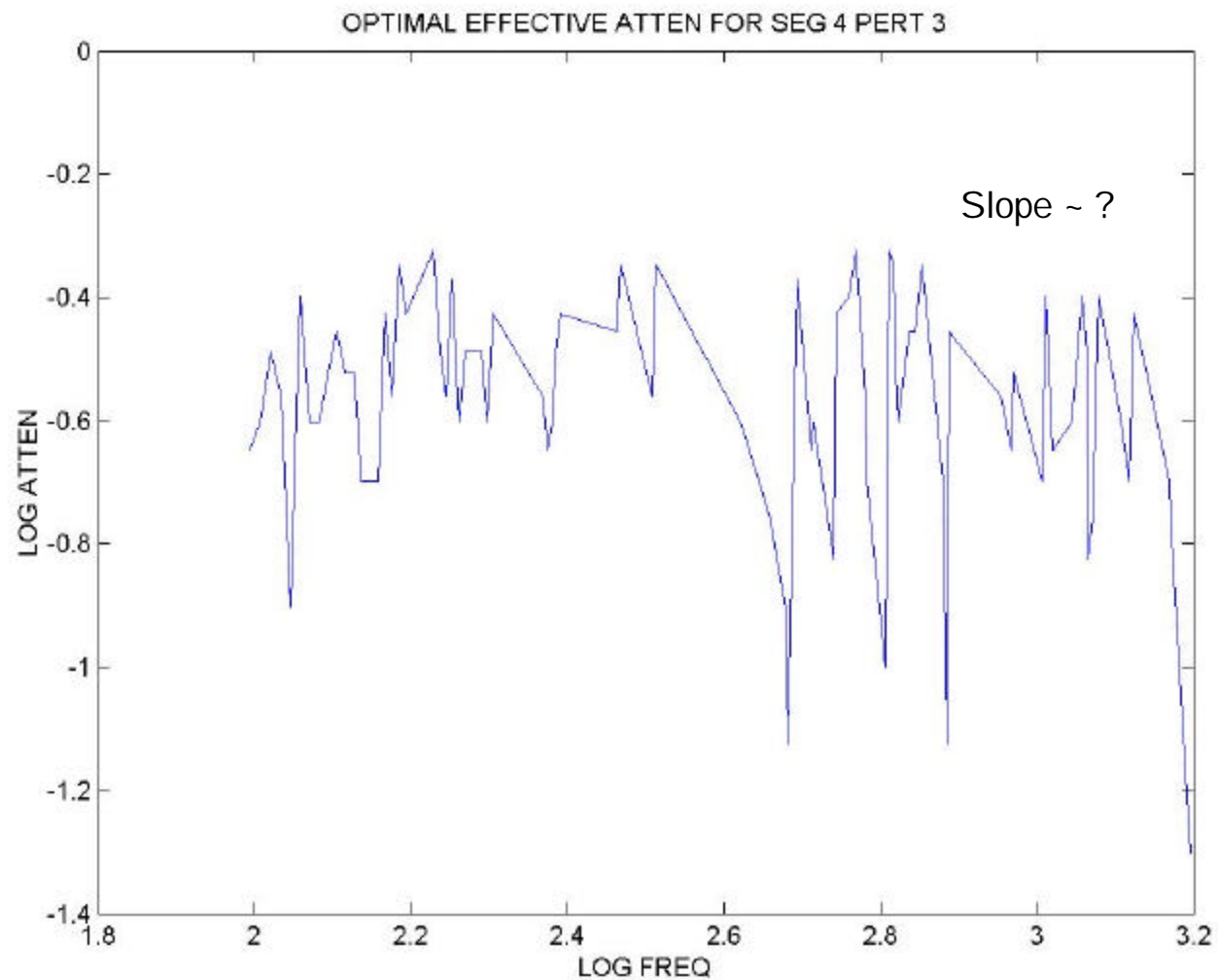
# Log-log analysis of Env 4, Pert 1



## Log-log analysis of Env 4, Pert 2



## Log-log analysis of Env 4, Pert 3



# Summary – Part II

- Cost function can be critical to inversion!
- Total energy in field for low ( $< 100$  Hz) and high ( $> 1$  kHz) frequencies do not exhibit nonlinear attenuation effect for these perturbations. Mid-frequency (100 – 1000 Hz) do exhibit nonlinear dependence for some perturbations,  $\alpha \sim f^{(1.7 \rightarrow 2.0)}$ .
- Gradient in sediment sound speed and basement interface roughness affect total energy the most.
- Subbottom variability still suggests reduction in power law dependence,  $\alpha \sim f^{0.6}$ , over low frequencies.

# Summary – Part II

- Previous conjecture still valid, and may be interpreted physically as indicated below

